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# Integration and Control of Morphing Wing Structures for Fuel Efficiency/Performance

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# Pressure Adaptive Structures for Distributed Control of Morphing Wing Vehicles

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- Project Overview
  - Objectives
  - Background
  - Challenges
  - Concepts: PAHS and DMoWCs
  - Infusion path
  - Approach
  - Phase 1 Status
- Technical Details and Accomplishments
  - Part 1: Pressure adaptive honeycomb
  - Part 2: Distributed decentralized control
  - Part 3: Small-scale morphing wing prototype study
- Summary



# Pressure Adaptive Structures for Distributed Control of Morphing Wing Vehicles

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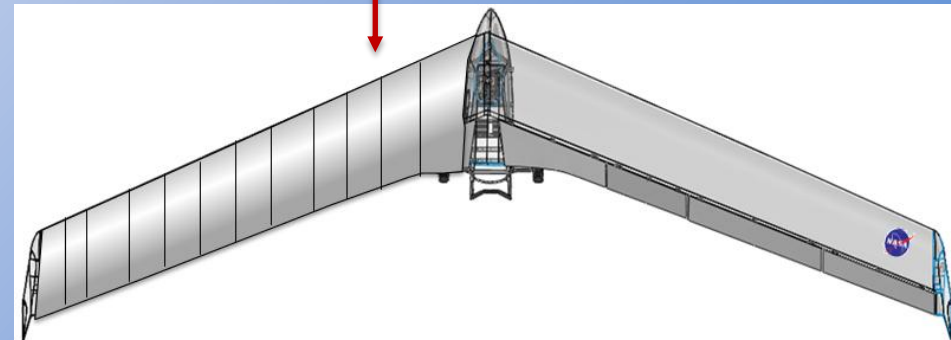
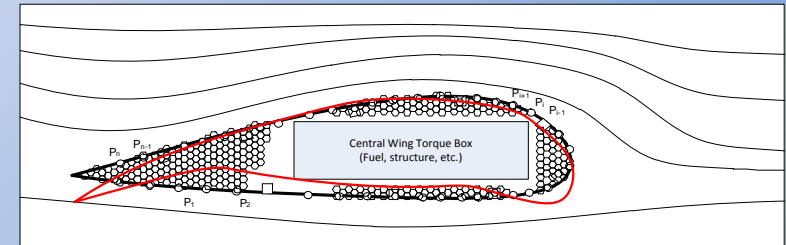
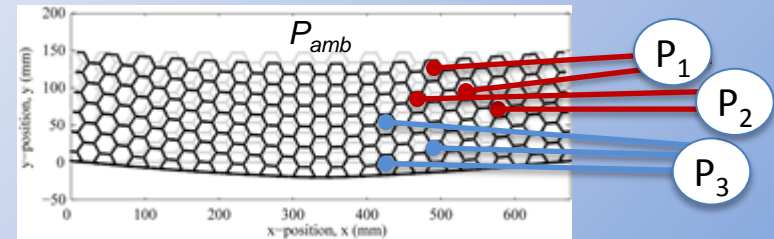
- Objective
  - Investigate GN&C of vehicles through distributed morphing wing shape control using pressure adaptive honeycomb structures (PAHS) towards drag reduction, increased efficiency, and enhanced capabilities.
  - Airfoil shape morphing to replace traditional control surface actuators
  - Distributed system of smart actuators (locally-sensing, locally-affecting, autonomous and multifunctional)
  - Combine classical modeling/control approaches with massively paralleled computing capability
- Innovation
  - Concept of Pressure Adaptive Wing System (PAWS) studies two novel approaches:
  - Pressure Adaptive Honeycomb (**PAHS**) morphing structures
  - Distributed and decentralized flight control through a Distributed Morphing Wing Control System (**DMoWCs**)
  - Studies replacing flight control surface actuation with intelligent distributed morphing
- Ties into NASA Aeronautics goals
  - Enabling lighter-weight multifunctional wing structures
  - Reduced drag and increased efficiency
  - Mission and configuration adaptation
  - Increased safety and robustness



# Distributed Control through Pressure Adaptive Structures

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- Pressurized honeycomb structure with active/passive bladders
- Install in the wing in place of standard control surface actuators to affect wing shape change
  - Adaptive intrados/extrados wing surfaces, trailing and leading edge deflection
- Control sections independently for vehicle flight guidance and control
- Distribute and decentralize control authority to local sections (architecture) – smart sensing, distributed control intelligent, actuation autonomy
- Blend rigorous control techniques with modern massively-paralleled many-core technology





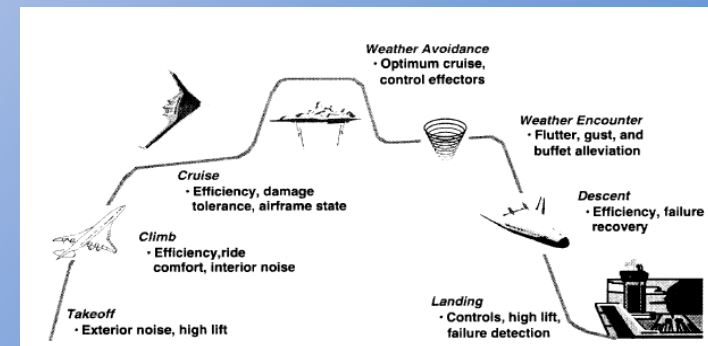
# History and Benefits

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- Long history of morphing wing research since 1920 (at least)
  - Parker's variable camber wing (Parker, 1920), NASA Aeroelastic Active Wing (1990's), Supercritical Mission Adaptive Wing (Powers, 1997), NASA Morphing Aircraft Program (Wlezien, 1998), DARPA/AFRL/NASA Smart Wing Project (Kudva, 2004), ...
  - Many recent surveys (Barbino 2011, Sofla 2010, Reich 2007, Kudva 2004,...)
  - Studies for distributed local shape actuation concepts in terms of aerodynamic-effect and feasibility, showing increase of benefits over global actuation
  - Studies show numerous benefits to actively controlling wing shape throughout the mission/flight regime

## *Benefits includes...*

... increased aerodynamic efficiency, drag reduction and enhanced lift-to-drag performance, enhanced maneuverability, reduced fuel consumption, increased actuator effectiveness, decreased actuator power requirements, increased control robustness, control redundancy, shorter required takeoff/landing length, flutter and stall mitigation, reduced airframe noise, increased stability and reduced stall susceptibility, ...



*Figure: Application of shape morphing technology (Wlezien, 1998)*





# Challenges and Needs

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- Actuation materials and scaling of mechanisms
  - Challenges in scaling of small laboratory or small-vehicle mechanism concepts
  - Challenges in materials certification
  - PAHS modeling (kinematics, dynamics)
  - Controlling shapes through PAHS
  - Optimization for multi-objective, multi-constrained flight control
  - Design models and system-level tradeoffs (MDAO)
- Distributed morphing control challenges
  - Need to show that decentralized shape control is feasible and promising
  - Many advanced large-scale nonlinear control concepts are difficult to validate
  - Lack of adequate models for control development for distributed concepts
  - Lack of control systems-level integration studies, integrating distributed morphing as primary actuator into a flight control system
  - Lack of system-level vehicle integration data/models for designers or for including into an design/MDAO process



# Pressure Adaptive Honeycomb

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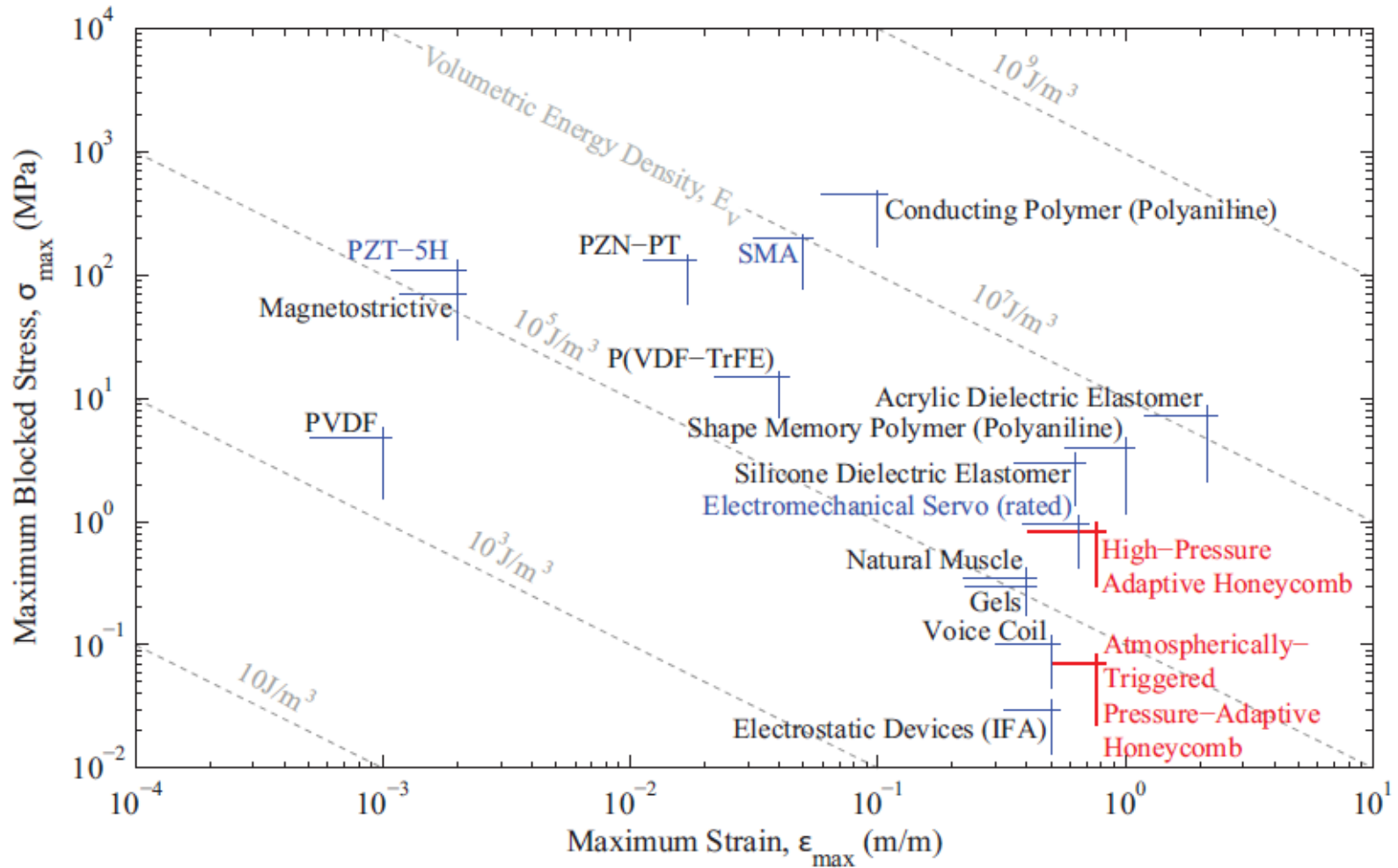
- Pressure Adaptive Honeycomb Structures (PAHS)
  - PAHS actuation has been demonstrated on small scale lab tests
  - Shown to have favorable characteristics in comparison to other types of morphing actuation (such as SMA's, piezoelectric)
  - Potential for distributed control
  - Complexity in application – structural design, kinematics/dynamics that describe actuation input to shape, multiple inputs
  - Need models for shape control, need larger-scale prototype for validation of initial study
- Apparent Benefits (from small-scale prototype)
  - Enabling lighter-weight multifunctional wing structures
  - Capable of "huge" (50+%?) strains
  - Fully proportional, easily controlled
  - Stiff & strong enough to handle "real" loads
  - Lighter than conventional aircraft actuation systems
  - Faster than conventional aircraft actuation systems
  - Less costly than conventional aircraft actuation systems
  - Does not require dedicated power system/consumption
  - Self-diagnostic with self-repair capability
  - Certifiable under FAR 23/25, 27/29

10 lbs



# PAHS Compared to Adaptive Materials

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Based on initial study of laboratory prototype

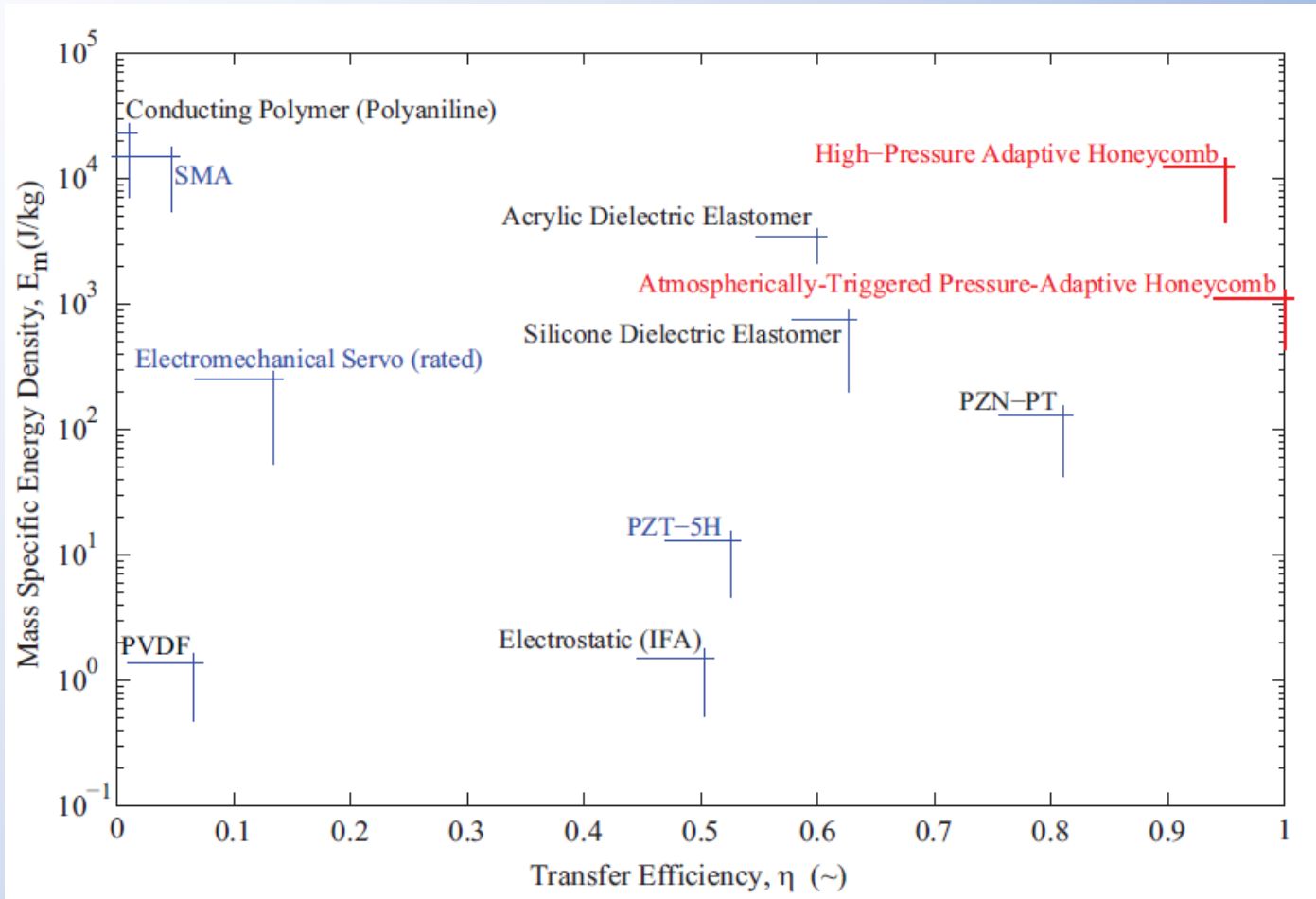
Vos, Barrett. "Topology Optimization of Pressure Adaptive Honeycomb for a Morphing Flap", SPIE Smart Structures, San Diego, CA. March 2011





# PAHS Compared to Adaptive Materials

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Based on initial study of laboratory prototype

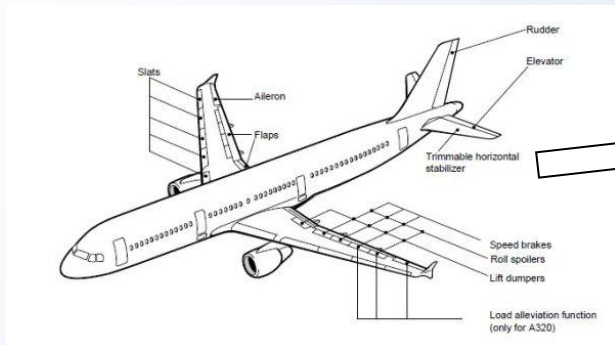
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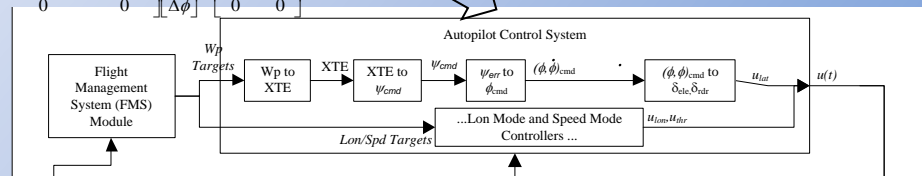
# Challenges with Traditional Flight Control Modeling and Design

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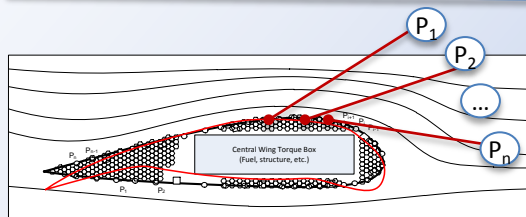
Simply, linearize, assume, simplify some more until a simple input-output mapping is derived  
Valid for only small 'deviations' around trim state  
Linearize around as many trim-states as possible  
Make system look like a simple spring-mass-damper (bypasses fluid response)



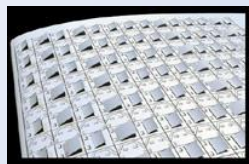
$$\frac{d}{dt} \begin{bmatrix} \Delta v \\ \Delta p \\ \Delta r \\ \Delta \phi \end{bmatrix} = \begin{bmatrix} Y_v & Y_p & - (u_0 - Y_r) & g \cos \theta_0 \\ L_v & L_p & L_r & 0 \\ N_v & N_p & N_r & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta v \\ \Delta p \\ \Delta r \\ \Delta \phi \end{bmatrix} + \begin{bmatrix} 0 & Y_{\delta} \\ L_{\delta a} & L_{\delta r} \\ N_{\delta a} & N_{\delta r} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta \delta_a \\ \Delta \delta_r \end{bmatrix}$$



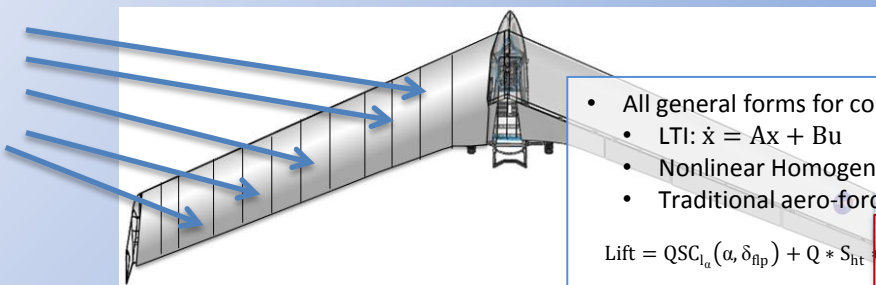
Control largely SISO loop-at-a-time cascades, indicative of classical control



Distributed shape changing concept



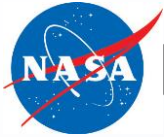
... or any distributed local actuation concept



- All general forms for control modeling are not satisfactory, eg.
- LTI:  $\dot{x} = Ax + Bu$
- Nonlinear Homogenous Form:  $\dot{x} = fH(x, t) + fF(u, t)$
- Traditional aero-forces/moment build up, eg:

$$\text{Lift} = QSC_{l_a}(\alpha, \delta_{flp}) + Q * S_{ht} * \frac{dC_l}{d\delta_{ele}} \delta_{ele} + \left( \frac{QSC}{2V} \right) \frac{dC_l}{d\alpha} \dot{\alpha} + \left( \frac{QSC}{2V} \right) * \frac{dC_l}{dq} \dot{q} \dots$$

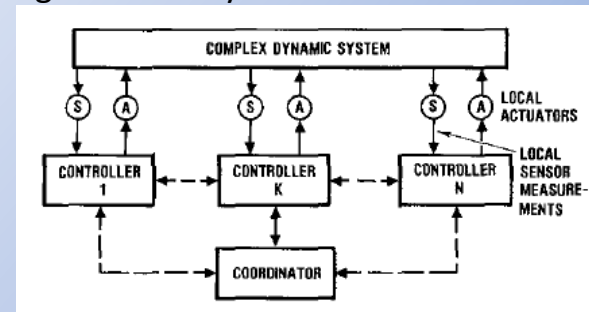
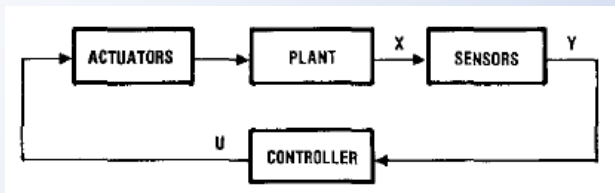
- Fundamentally a large-scale problem
- Nonlinearity, non-symmetry
- Complex actuation and dynamic coupling
- Large set of control inputs, large number of states
- Homogenous time-variance
- Fluid response cannot be simplified out of equations



# Decentralized Control Approach and Impact

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- DMoWCs : Distributed Morphing Wing Control System
  - Novel control approach for design of distributed flight control systems



Centralized Versus Decentralized (Sesak & Coradetti 1979)

- Scalable massively parallelizable framework for multi-objective constrained optimization
- Modeling and controlling spatially-invariant large-scale dynamic systems
- Distribution and decentralization using local controllers/sensors/actuators
- Incorporates into existing flight control architectures
- Can be verified using classical control techniques and metrics
- Proposed large-scale control-modeling approach applicable to any distributed actuator systems, captures nonlinearity, complexity, large-scale effects
- General framework for distributed heterogeneous smart-actuator control of large-scale systems
- Applying same architecture for research for smart-building control system research (NASA ARC Sustainability Base)



# Infusion Path to NASA ARMD Program

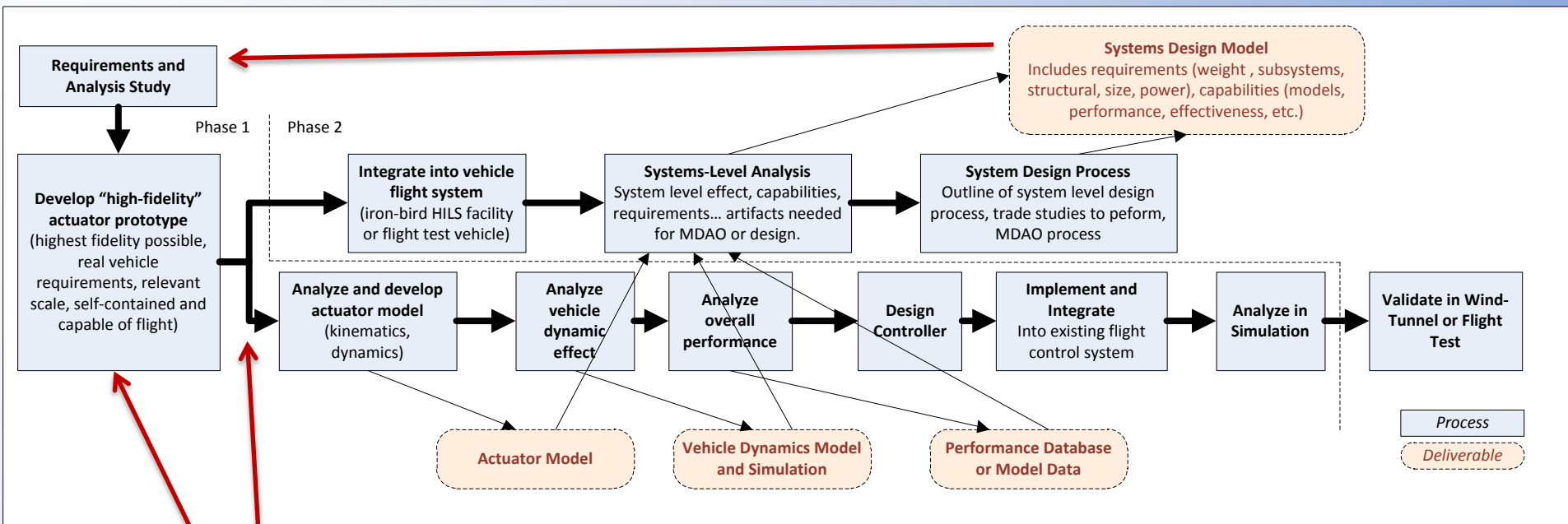
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- Phase 1 results show the approaches to both morphing and control are feasible
- Found support from partners in NASA and industry
  - Letter of support from NASA ARMD FW's ESAC (Elastically Shaped Aircraft Concept) task
  - Letter of support from Boeing Company, Research and Technology business unit
  - Letter of support from Cessna Aircraft Company, Co-PI from MLB company (UAV market)
- Infusion Path
  - Overall phase 2 goal is to advance the concept maturity to be incorporated into existing NASA projects and industry
  - Tests PAWS actuator at larger scale, applying DMoWCs in demonstration
  - Phase 2 will provide NASA/Boeing teams with regular updates, get regular feedback
- Benefits for NASA project
  - Actuator deliverables provides ESAC/Boeing project with new actuation possibility
  - Control models and framework provides new approaches to ESAC
  - Framework could allow ESAC to approach other NASA projects in related disciplines (eg smart-material projects) for collaboration



# Approach and Initial Plan

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1. Task plan dependency issue
2. Prototype requirements issue (what to build, effectiveness of flight testing without 'going through the loop' again)





**Requirements and Analysis Study**

**Phase 1**

**Develop “high-fidelity” actuator prototype**  
(highest fidelity possible, real vehicle requirements, relevant scale, self-contained and capable of flight)

**Phase 2**

**Integrate into vehicle flight system**  
(iron-bird HILS facility or flight test vehicle)

**Systems-Level Analysis**  
System level effect, capabilities, requirements... artifacts needed for MDAO or design.

**System Design Process**  
Outline of system level design process, trade studies to perform, MDAO process

**Analyze and develop actuator model**  
(kinematics, dynamics)

**Analyze vehicle dynamic effect**

**Analyze overall performance**

**Design Controller**

**Implement and Integrate**  
Into existing flight control system

**Analyze in Simulation**

**Validate in Wind-Tunnel or Flight Test**

**Added Task: Develop small/simple Phase 1 actuator (mini project)**

**Actuator Model**

**Vehicle Dynamics Model and Simulation**

**Performance Database or Model Data**

**Systems Design Model**  
Includes requirements (weight, subsystems, structural, size, power), capabilities (models, performance, effectiveness, etc.)

**Process**

**Deliverable**

Likely out of scope...



# Phase 1 Project Milestone Review

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ID	Modified Phase 1 Task	Status
1.0	PAWS Design and Requ. Study	Complete
2.0	PAWS Prototype Fabrication	On schedule
3.0	Control and Morphing Wing Survey	Complete
4.0	<b>Perform initial control feasibility / small-scale prototype study</b>	Complete
	Develop prototype small-scale actuator	
	Integrate into UAV, obtain flight test approval	
	Analyze and model actuator	
	Model and simulate flight dynamics	
	Develop prototype control system	
	Conduct simulation studies	
5.0	PAH/UAS 6DOF M&S	Complete
	Develop mathematical modeling framework	
	Integrate into NASA UAS/PAWS	
6.0	DMoWC Baseline and Sim Integration	Complete
7.0	DMoWC Development and Testing	On schedule
8.0	Final Reporting, Phase 2 Planning	On schedule

*PAWS Prototyping  
(1.0 and 2.0, Led by KU Team)*

*DMoWCs Prototyping  
(3.0 to 7.0, Led by NASA Team)*

*Tasks in green were added.*



# TECHNICAL DETAILS AND ACCOMPLISHMENTS

## PART I – PAWS DEVELOPMENT

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Zaki H. Abu Ghazaleh  
Graduate Research Assistant  
AE/University of Kansas



# Phase 1 Highlights: PAWS Prototype Development

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- Summary: PAWS Prototype Development
  - Completed initial selection, requirements, airfoil study for the PAWS prototype
  - Selected morphing target for prototype
    - Identified high-lift takeoff and landing shape
    - High-lift airfoil shape provides 50% improvement of  $C_L$ -max
  - Completed fabrication of the outer structure of the PAWS
  - On track to deliver PAWS actuator to NASA Ames at the end of FY12, despite project start date delay due to funding issues
  - Successful Phase 1 delivery of prototype allows Phase 2 analysis
  - Phase 2 analysis will provide data for incorporation into design process/MDAO

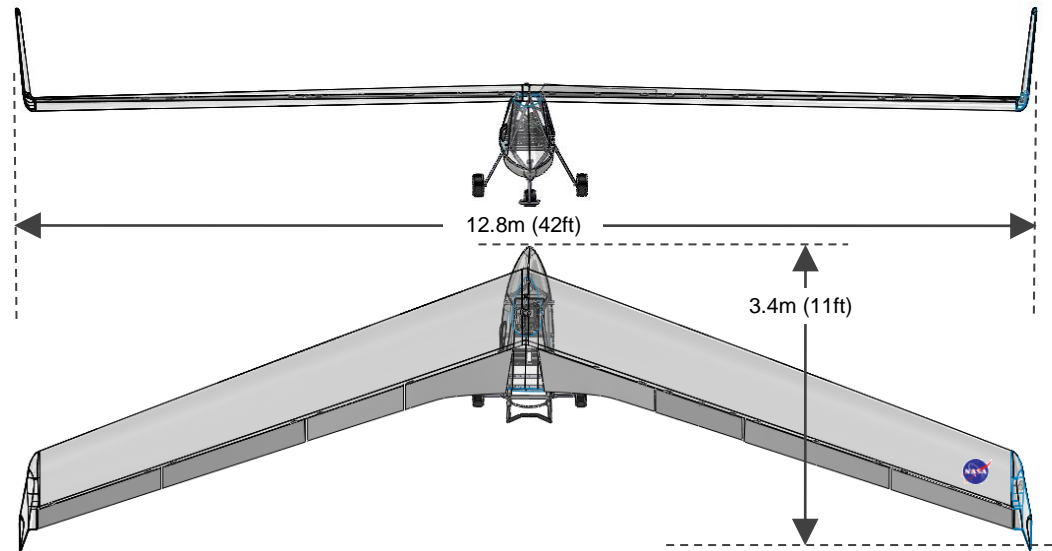


# Target Vehicle Selection: NASA Swift UAS

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## NASA Swift UAS Specifications

Wing Span:	12.8m (42ft)
Length:	3.4m (~11ft)
Wing area:	12.5 m <sup>2</sup> (136 ft <sup>2</sup> )
Aspect ratio:	12.9
Speed, Cruise:	45 knots (23 m/s)
Speed, Stall:	20 knots (10 m/s)
Speed, $V_{NE}$ :	68 knots (35 m/s)
MTOW:	150 kg (330 lbs)
Payload Weight:	100kg (220lbs)



- Needed a vehicle to derive integration and performance requirements, needed a vehicle with existing models and simulations for analysis, needed a vehicle at a manned-aircraft scale
- Swift UAS is a converted high-performance glider capable of carrying two-man payload
- Unique UAS size and payload capacity for low cost
  - Weight limited due to NASA UAS Risk Cat. 2 (medium-size)
  - Designed to safely test experimental controls, full system redundancy
- Flying-wing configuration exhibits similar challenges faced by proposed future aircraft design concepts
- Significant amounts of data available, directly accessible by PI

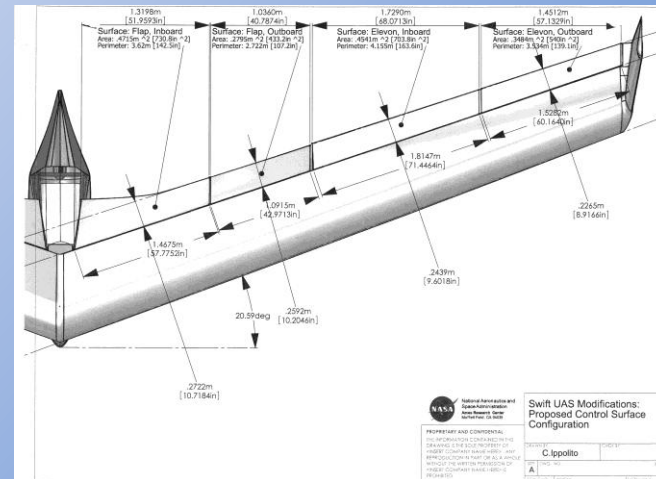
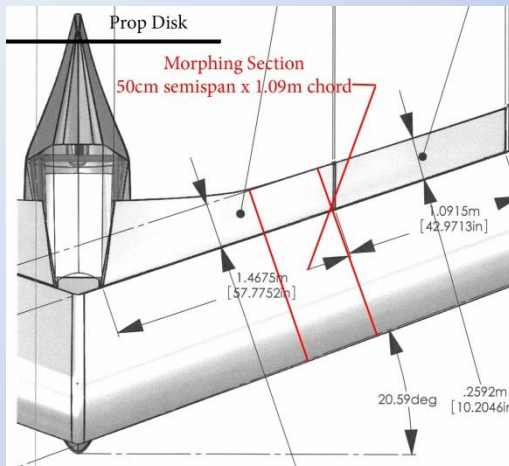




# Phase 1 Highlights: PAWS Prototype Development

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- Initial design and requirements study
  - Find ‘morphing target’ as shape requirement for KU prototype
  - PAWS prototype to be fitted to a Swift UAS wing section

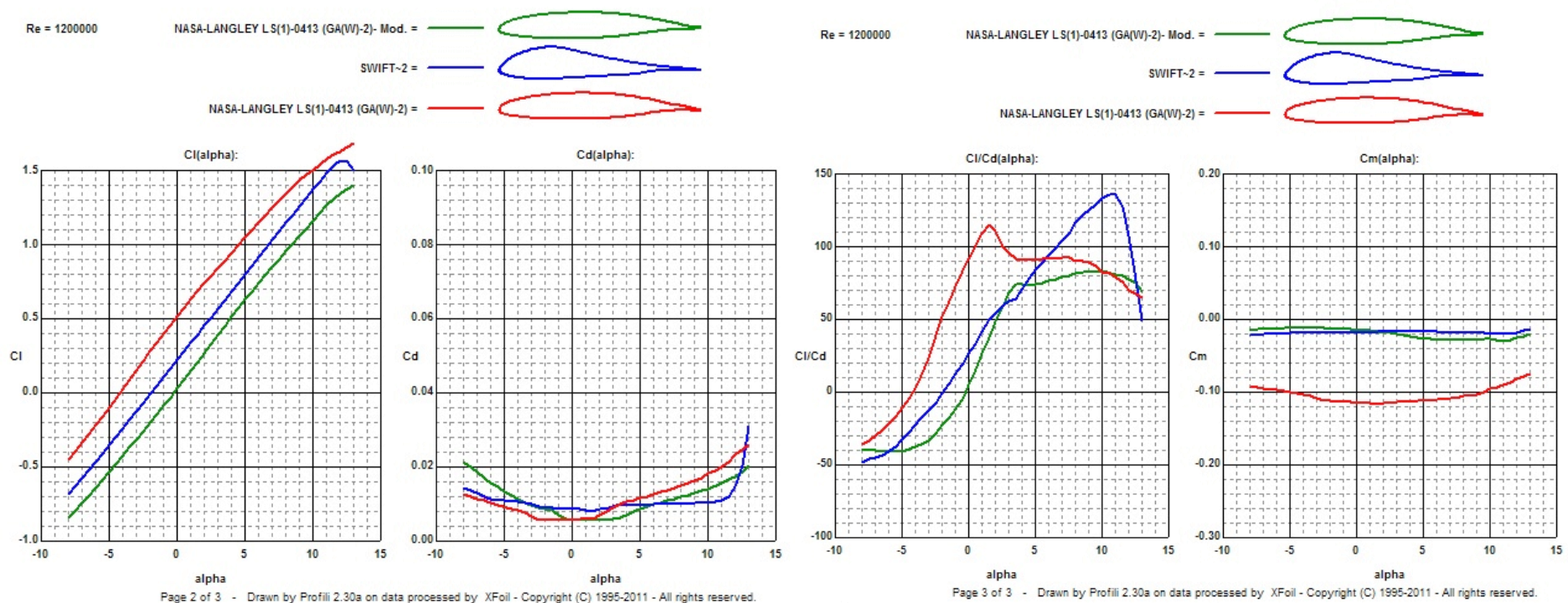




# Phase 1 Highlights: PAWS Prototype Development

NARI

- Comparison with NASA Langley LS(1)-0413, modified LS(1)-0413 appropriate for flying-wing

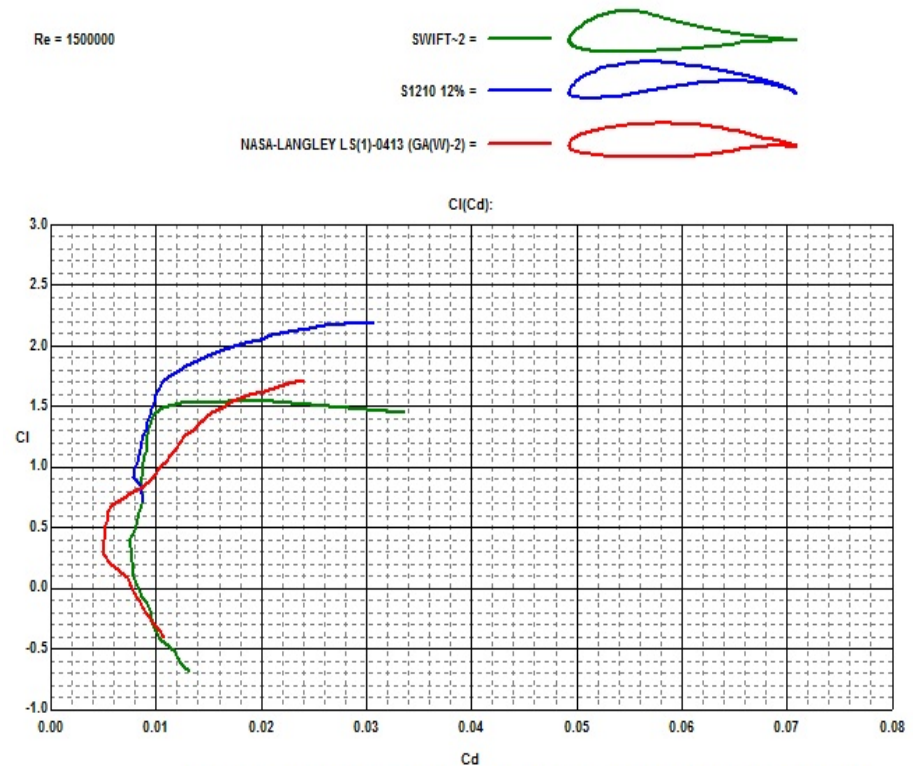
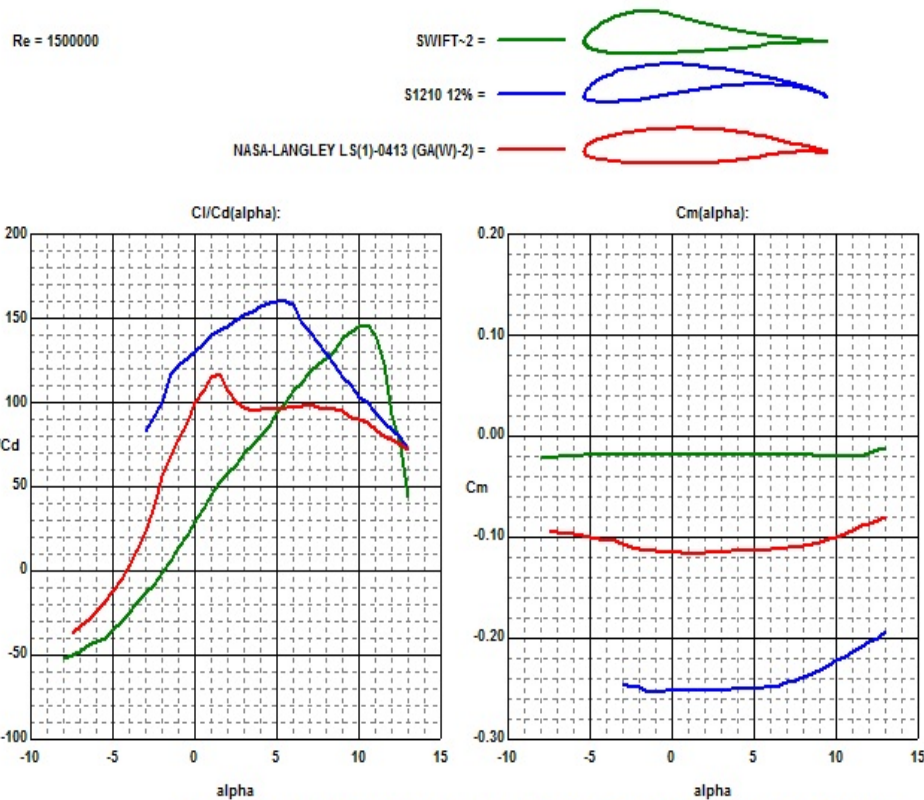




# Phase 1 Highlights: PAWS Prototype Development

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## – Comparison with Selig 1210



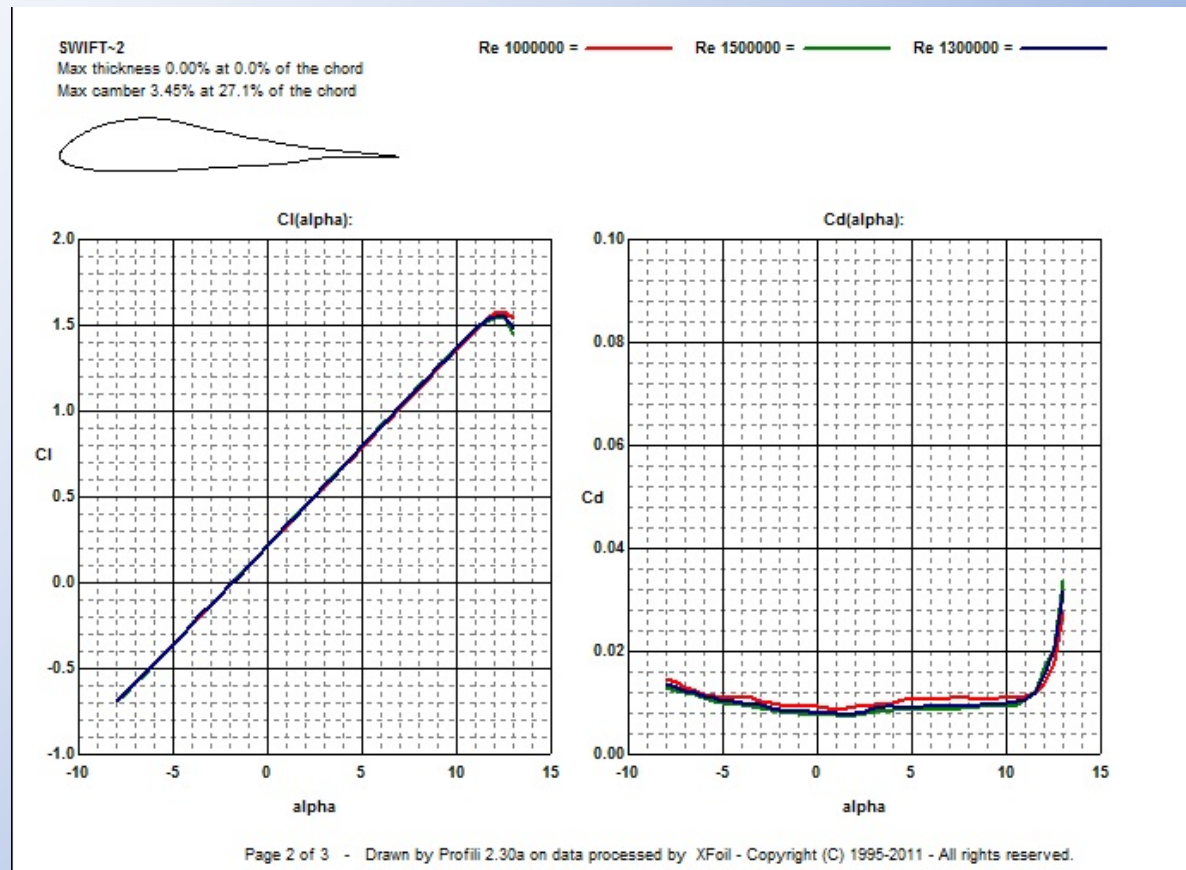




# Phase 1 Highlights: PAWS Prototype Development

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- Swift airfoil performance sweep with respect to  $R_n$

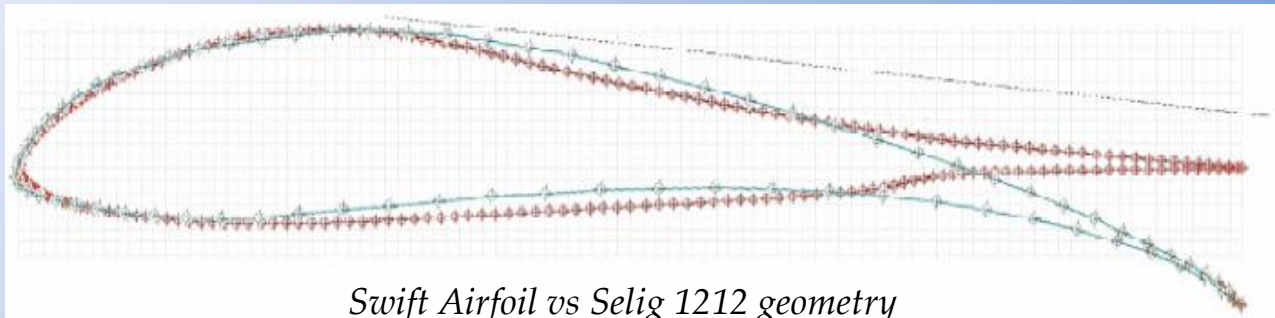




# Phase 1 Highlights: PAWS Prototype Development

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- Swift to Selig 1212 selected as morphing target endpoints
- Prototype requirement
  - Morph between the Swift airfoil in cruise to the Selig 1212 during takeoff and landing
  - Cruise section L/D in cruise will top 140
  - Takeoff/landing  $C_{lmax}$  values will approach 2.2 (nearly 50% improvement)
- Comparison of Swift Airfoil with Selig 1212 geometry
  - Leading edge geometric similarities, trailing edge and camber deflection
  - Allows wing torque box to be unmodified



*Swift Airfoil vs Selig 1212 geometry*





# Phase 1 Highlights: PAWS Prototype Development

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What is  $C_{L-max}$  implications for lightweight high-aspect ratio wings?

Estimated implications for LSA\* based on a 20% increase of clean  $C_{Lmax}^{**}$

- 17% reduction in wing wetted area
- 20% increase in aspect ratio
- 10% increase in L/D
- 8% reduction fuel burn and DOC at constant range
- 1.5% decrement in TOW and purchase price at constant range

\* 45kts flaps-up stall requirement

\*\* Based on: Roskam "Airplane Design," part I, II, V, and VIII, and Cessna 162 Skykatcher Data



# Phase 1 Highlights: PAWS Prototype Development

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- Constructed wing test section
- Below: prototype prior to fitting with adaptive honeycomb cells



Figure 10 110cm Chord x 50cm Semispan Morphing Wing Section Prototype



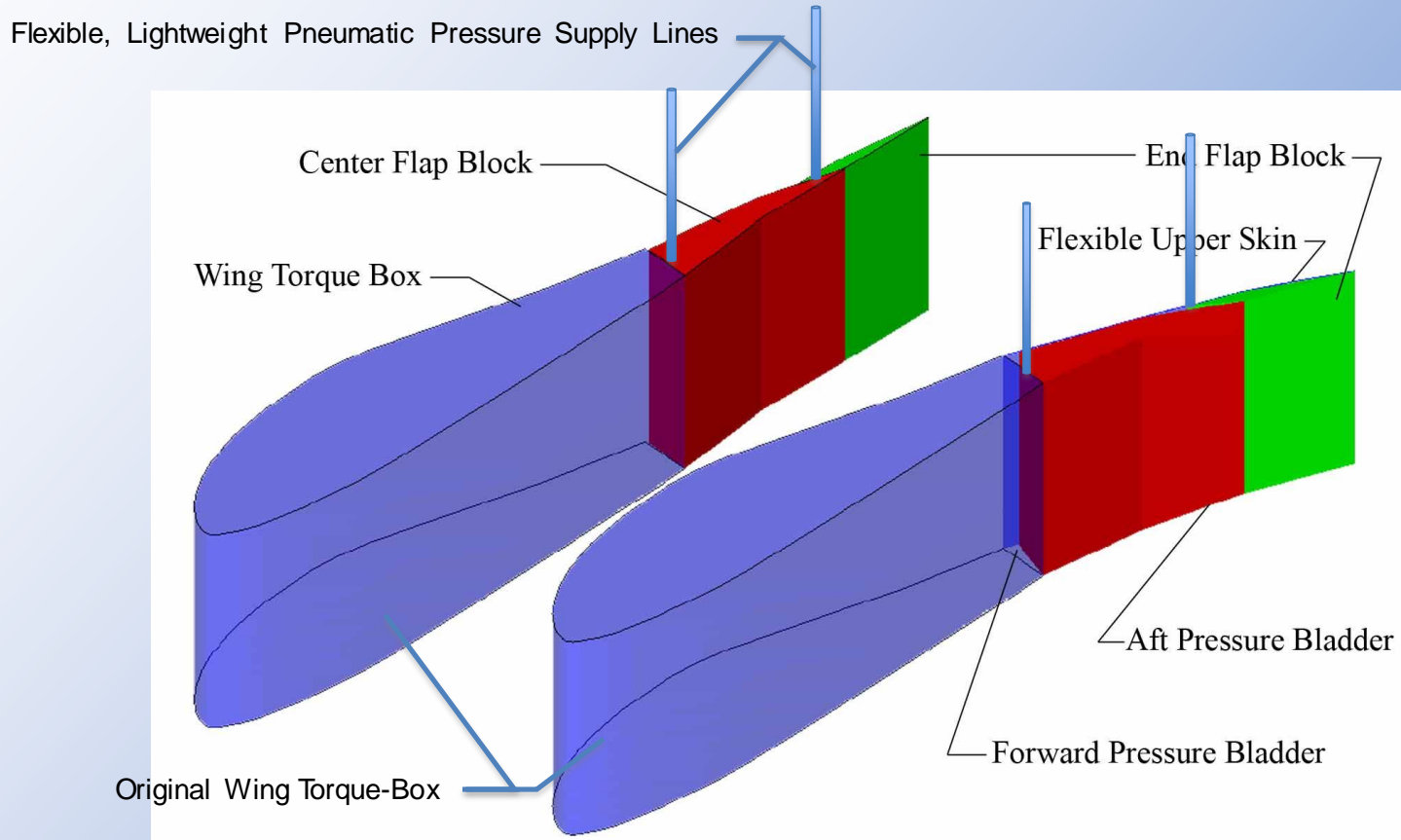
*Unmorphed Swift Airfoil to morphed Selig 1212 Airfoil  
(1.1m Chord x 50cm Semispan Airfoil Section)*



# Phase 1 Highlights: PAWS Prototype Development

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- Prototype design schematic for Swift to Selig 1212 morphing

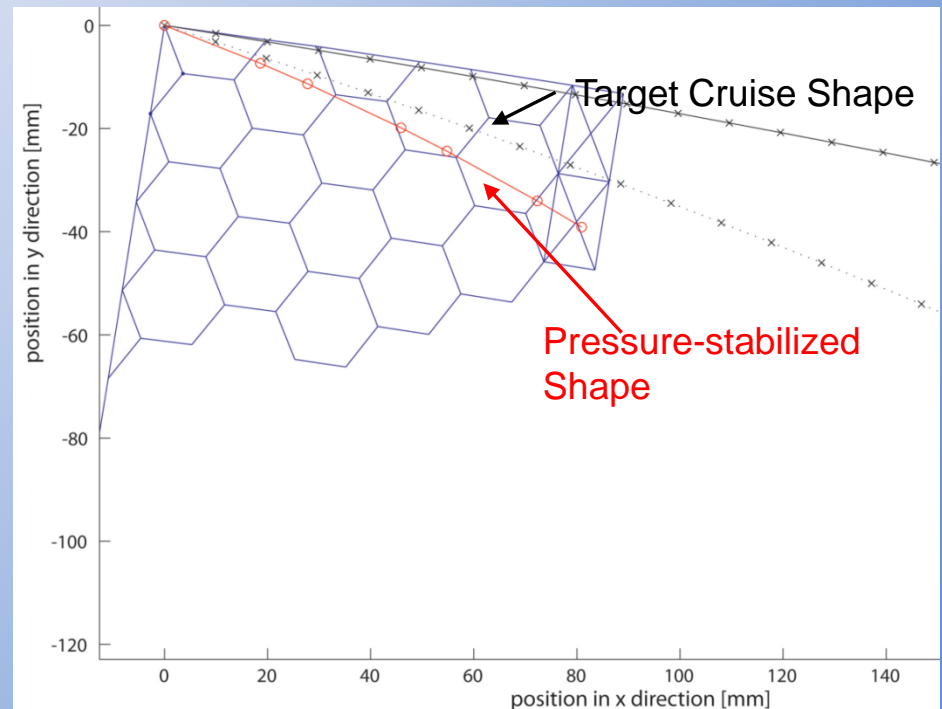
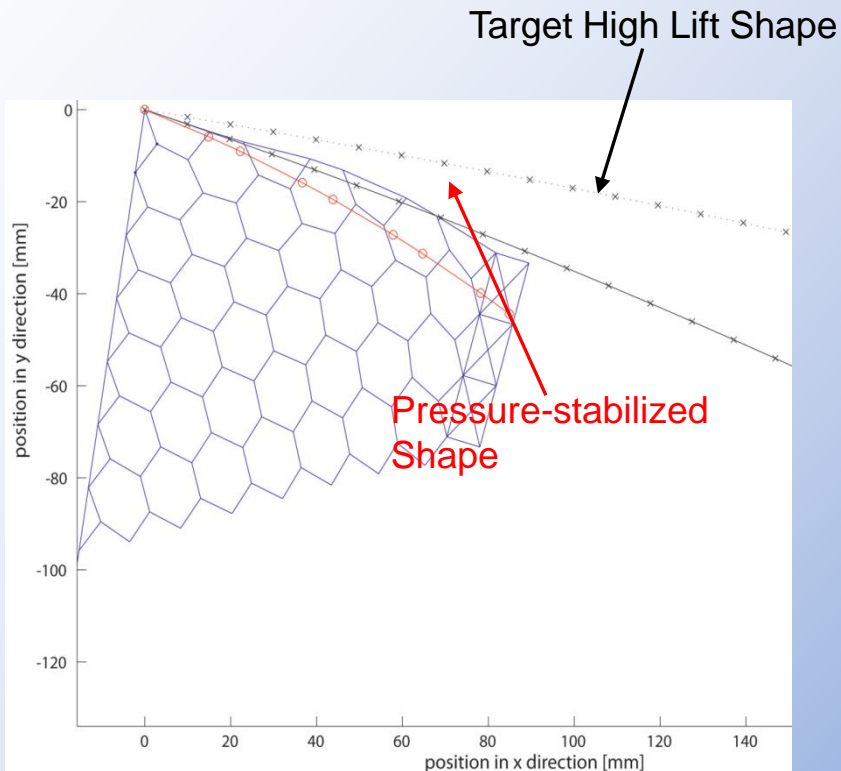




# Phase 1 Highlights: PAWS Prototype Development

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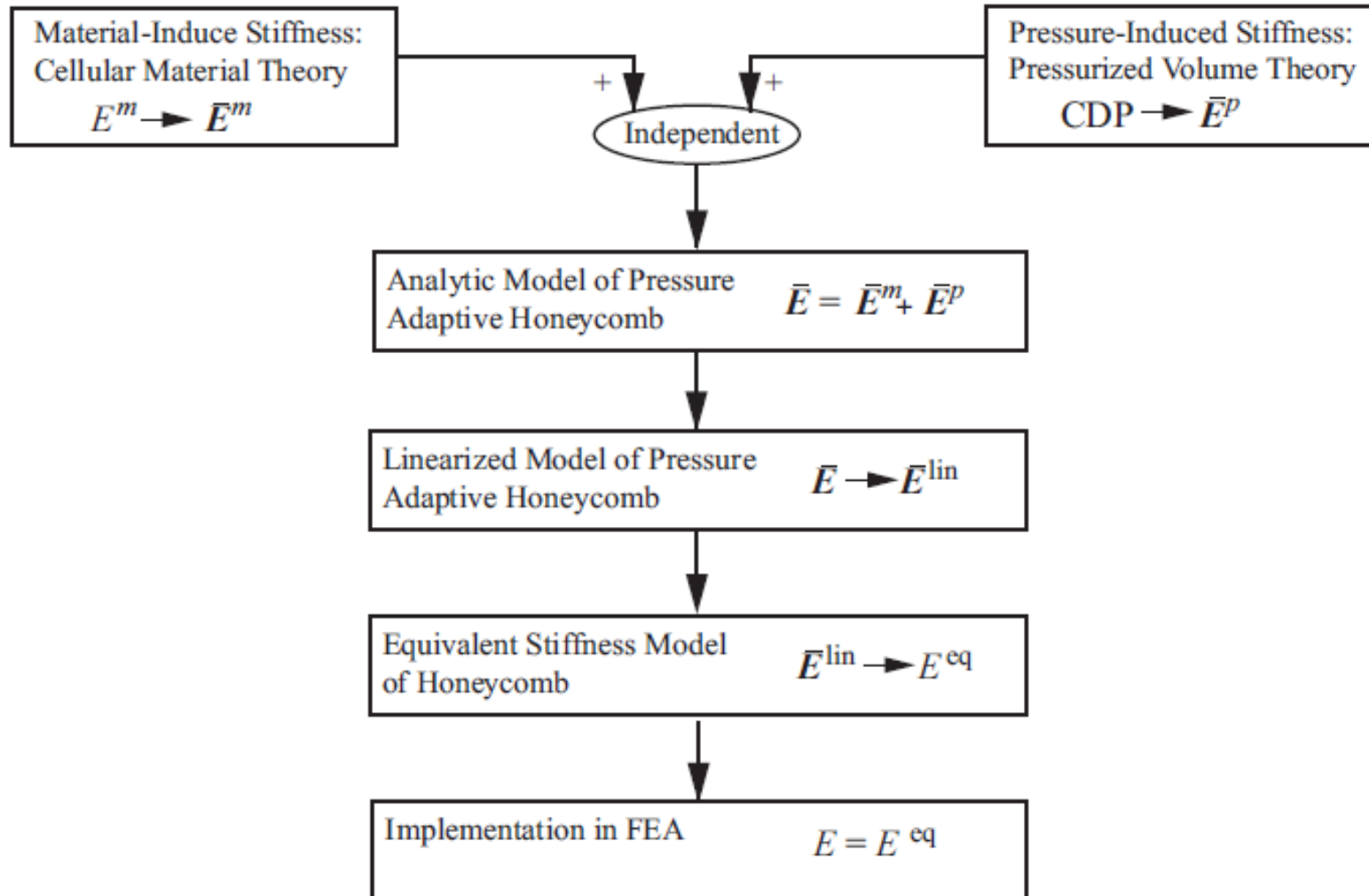
- PAHS modeling for shape control





# Theoretical Characterization

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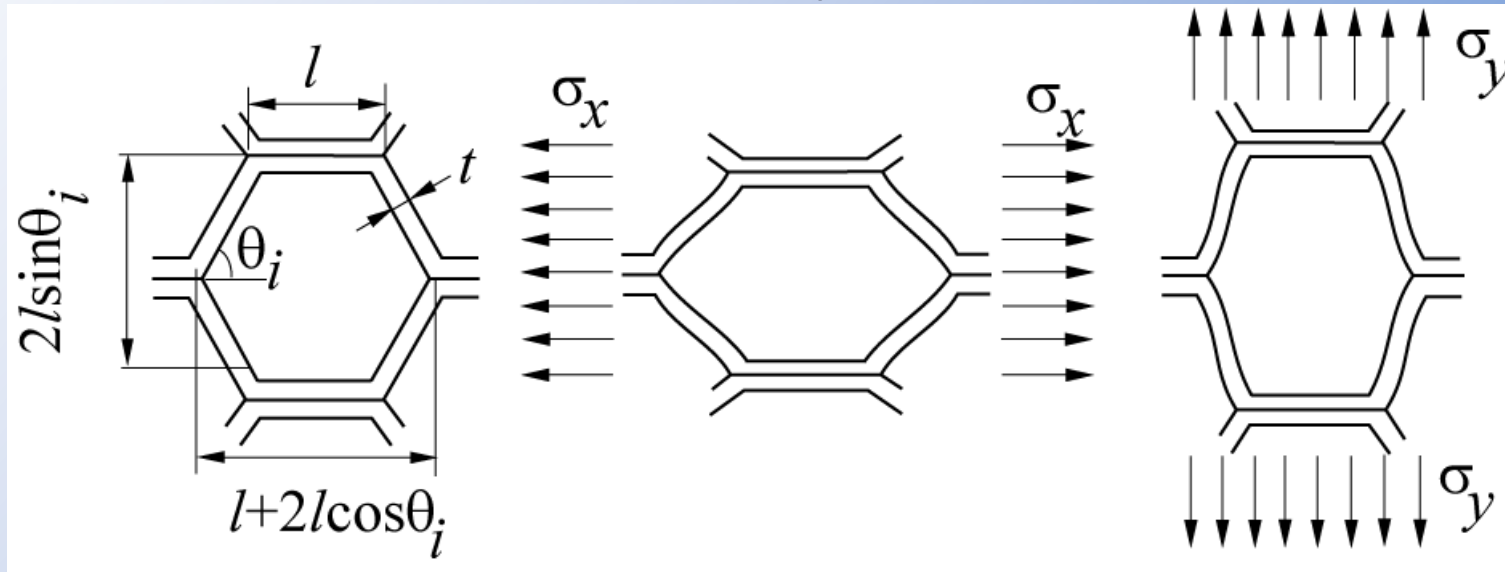
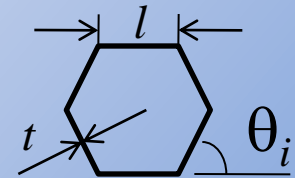
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# Linear-Elastic Honeycomb

Cellular Material Theory (CMT) after Gibson *et al.* 1988

Considerations:

- Only valid for small thickness-to-length ratio
- Only valid for +/- 20% of strain
- Linear stress-strain relationship





# Theoretical Characterization

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Linear model for honeycomb stiffness moduli:

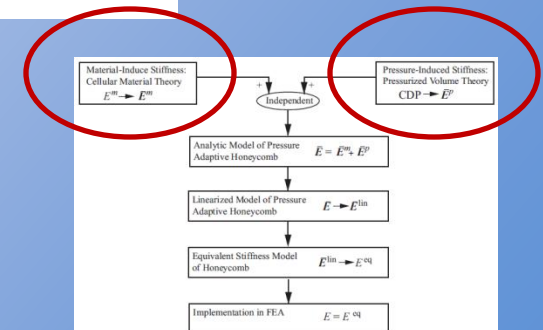
$$\bar{E}_x^m = E^m \left( \frac{t}{l} \right)^3 \frac{\cos \theta_i + 1}{\sin^3 \theta_i} \quad \text{and} \quad \bar{E}_y^m = E^m \left( \frac{t}{l} \right)^3 \frac{\sin \theta_i}{(1 + \cos \theta_i) \cos^2 \theta_i}$$

To find pressure-induced stiffness moduli:

$$W_{use} = \int_{V_i}^V p dV - p_a(V - V_i) \quad \text{and} \quad W_{ex} = \int_s F ds$$

Assumptions:

- Rigid members connected by hinges
- Constant pouch-to-hexagon volume ratio
- No friction forces between pouch and wall





# Theoretical Characterization

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Global stress-strain relations:

@ constant pressure:

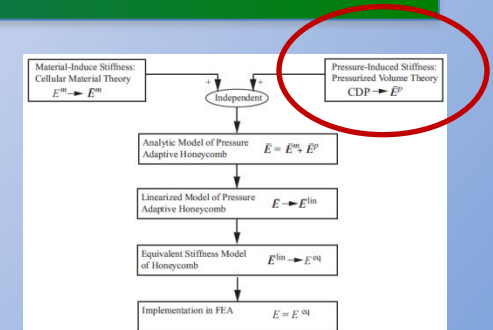
$$\sigma_x = \frac{1}{l^2(1 + \cos \theta_i)} \times \frac{(p - p_a)(V - V_i)}{\sin \theta - \sin \theta_i} \quad \text{and} \quad \sigma_y = \frac{1}{l^2 \sin \theta_i} \times \frac{(p - p_a)(V - V_i)}{\cos \theta - \cos \theta_i}$$

@ constant mass:

$$\sigma_x = \frac{1}{l^2(1 + \cos \theta_i)} \times \frac{mRT \ln(V/V_i) - p_a(V - V_i)}{\sin \theta - \sin \theta_i} \quad \text{and} \quad \sigma_y = \frac{1}{l^2 \sin \theta_i} \times \frac{mRT \ln(V/V_i) - p_a(V - V_i)}{\cos \theta - \cos \theta_i}$$

with

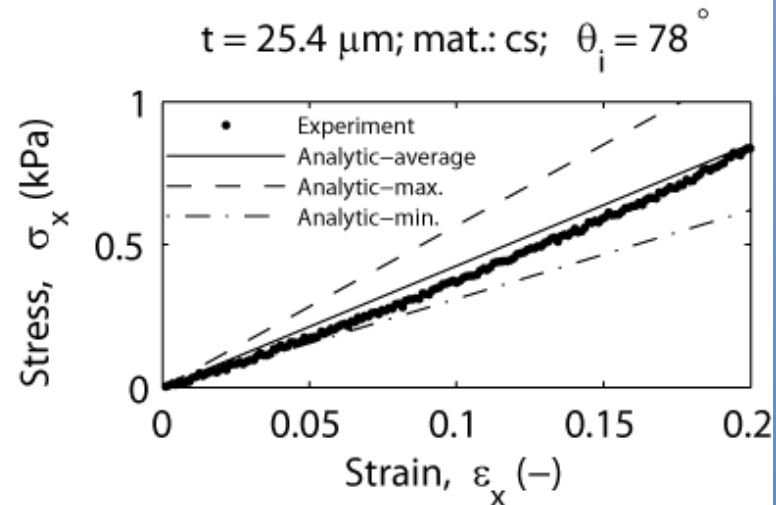
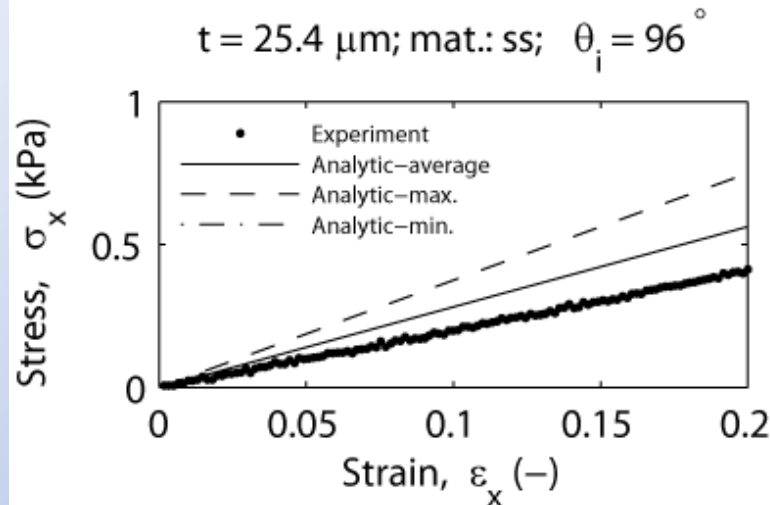
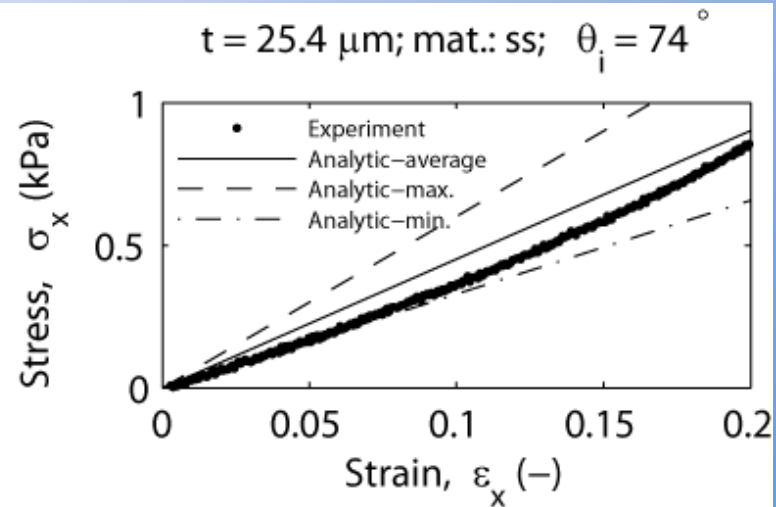
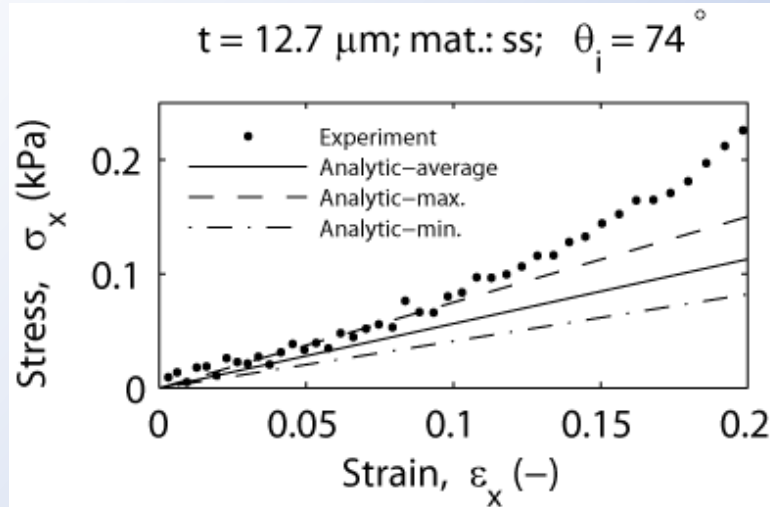
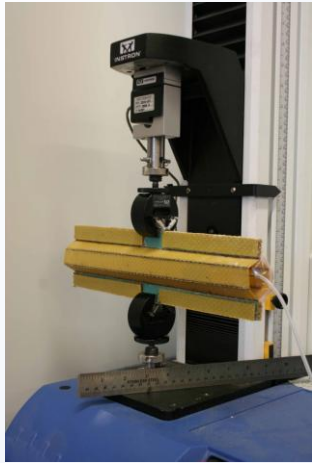
$$V = \zeta l^2 (1 + \cos \theta) \sin \theta$$





# Four-Cell Tensile Test of Steel Honeycombs (cont.)

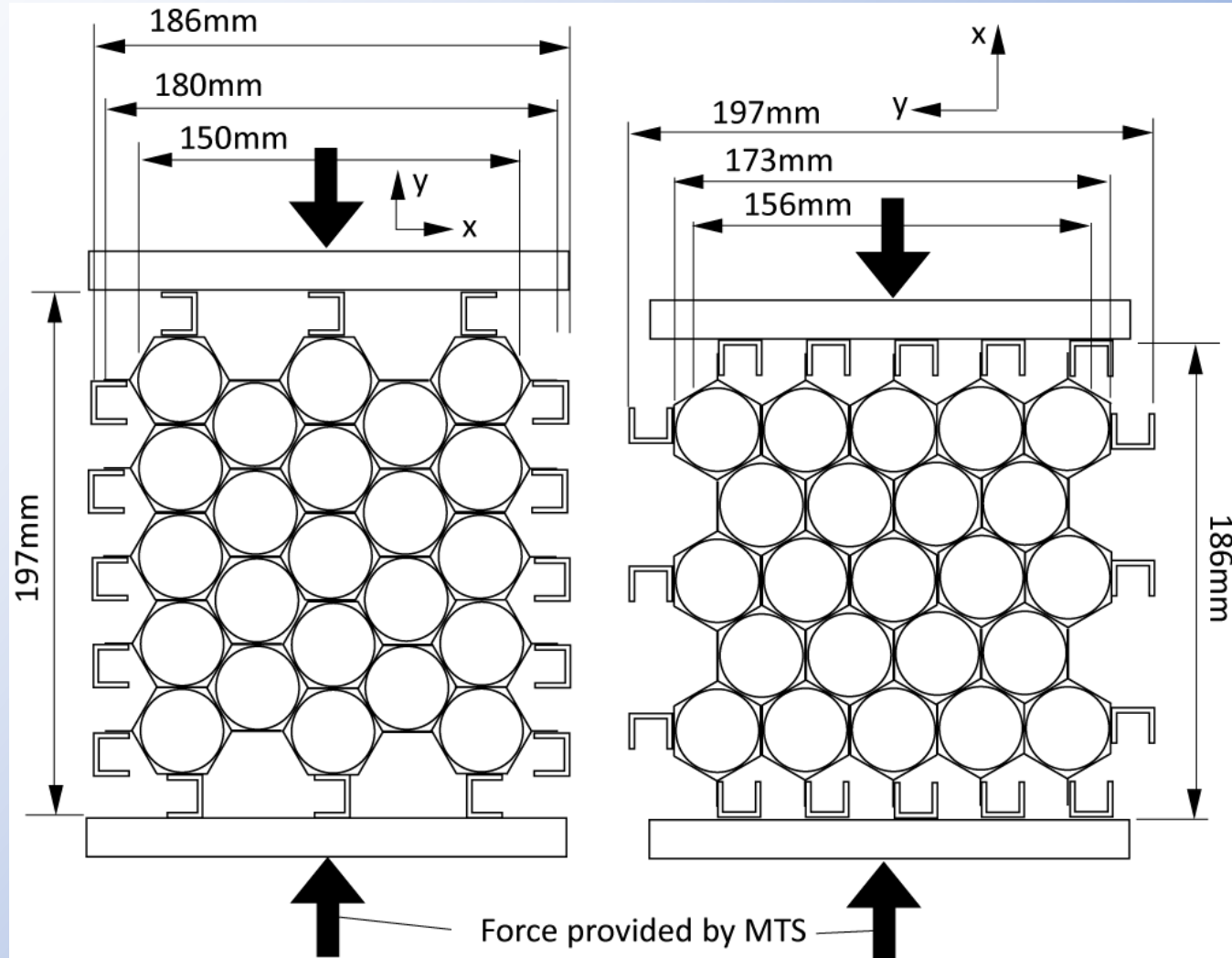
NARI





# Multi-Cell Compression Test (cont.)

NARI



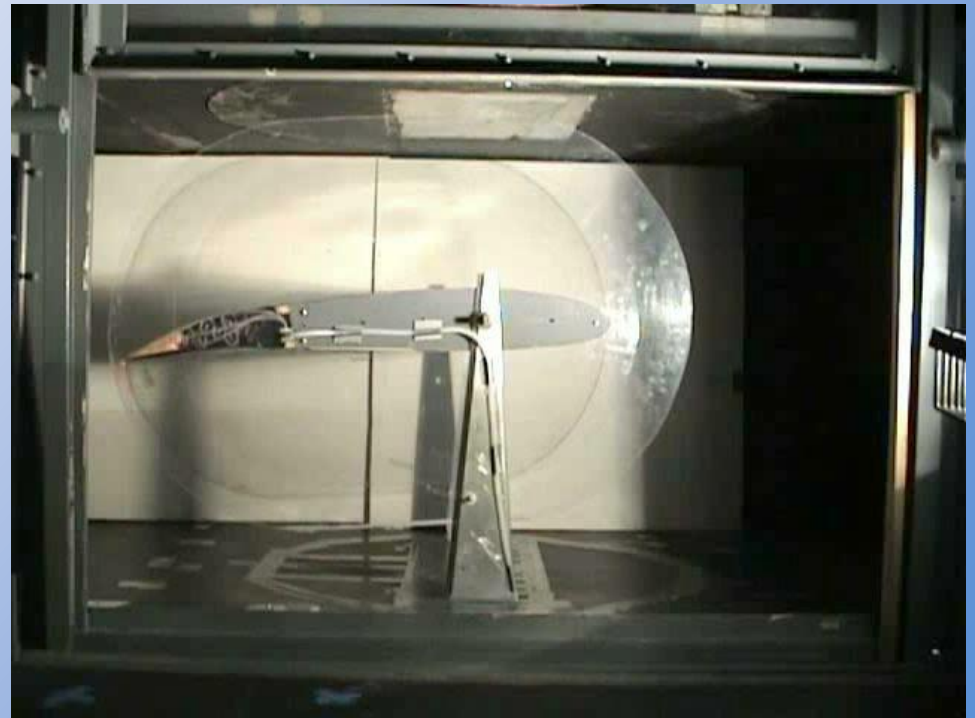




## Phase 1 Highlights: PAWS Prototype Development

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- Installation is currently underway on schedule for completion at the end of Phase 1





# TECHNICAL DETAILS AND ACCOMPLISHMENTS

## PART II – DMOWCS DEVELOPMENT

Corey Ippolito (PI)  
NASA Ames Research Center  
Ph.D. Candidate, ECE/CMU

Jason Lohn, Ph.D.  
Associate Research Prof.  
Dept of Electrical & Computer Engineering  
Carnegie Mellon University

NASA Student Interns:

Vishesh Gupta  
Jake Salzman  
Dylan King



# Phase 1 Highlights

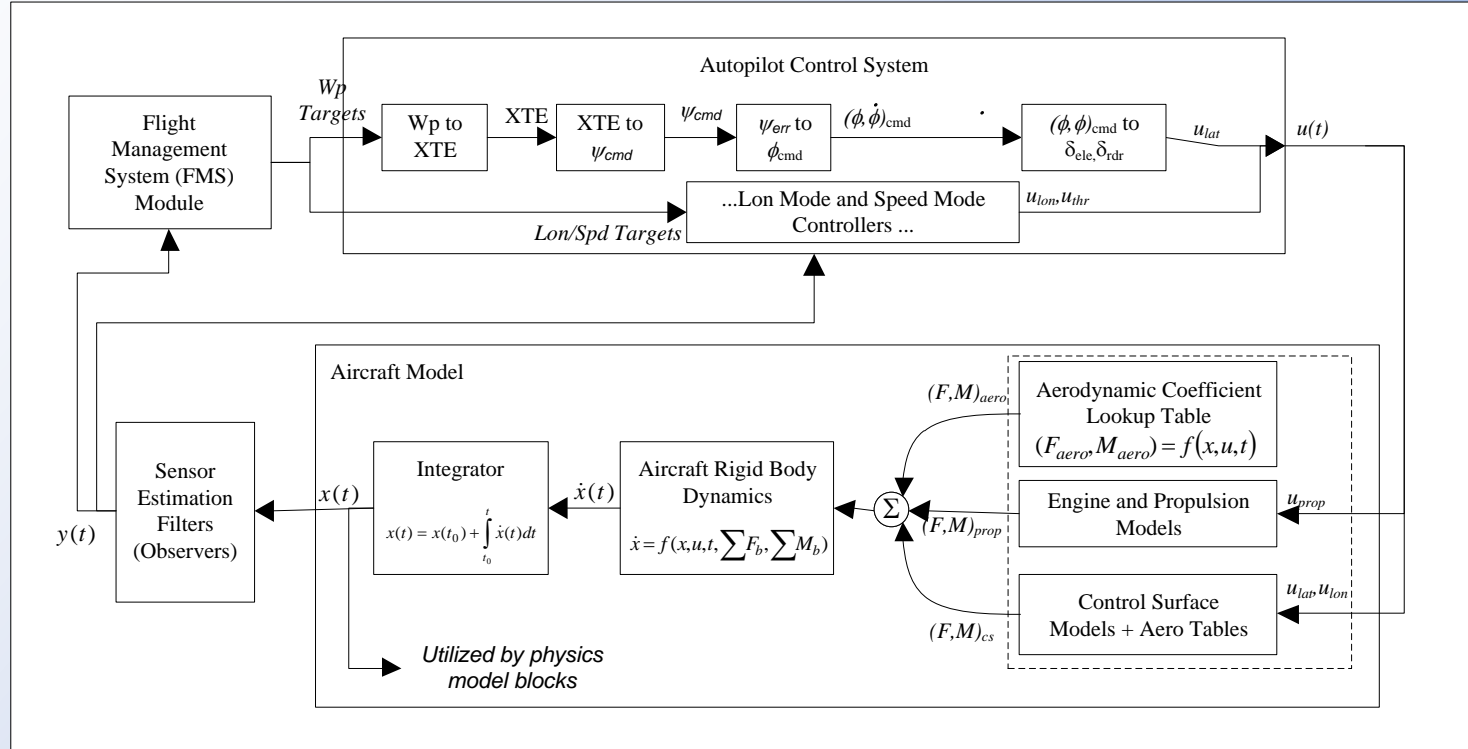
NARI

- Modeling and Simulation
  - Completed derivation of a parallelized mathematical model of the morphing wing vehicle utilizing a vortex-lattice solver that integrates into the vehicle's flight dynamics model.
  - Completing creation of a simulation environment that can be integrated into NASA's hardware in the loop simulation facility.
  - Conducted a study to investigate parallelization of the simulation model to increase run-time performance.
  - Parallelized and ported model to a many-core environment (NVIDIA CUDA GPU)



# Traditional Simulation and Control Architecture

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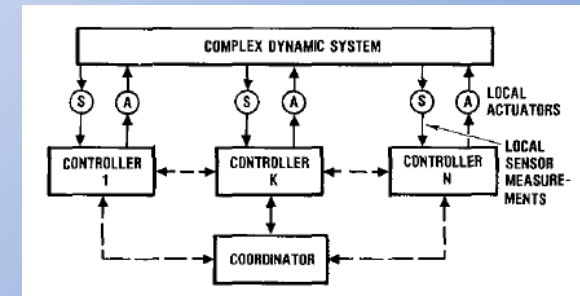
# Two Part Parallelized Model

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- Two components: topological model + physics-based element model

- Topological Model

- Graph-based model to describe phenomena physics and control system topology
- Variable granularity definition with variability in structure



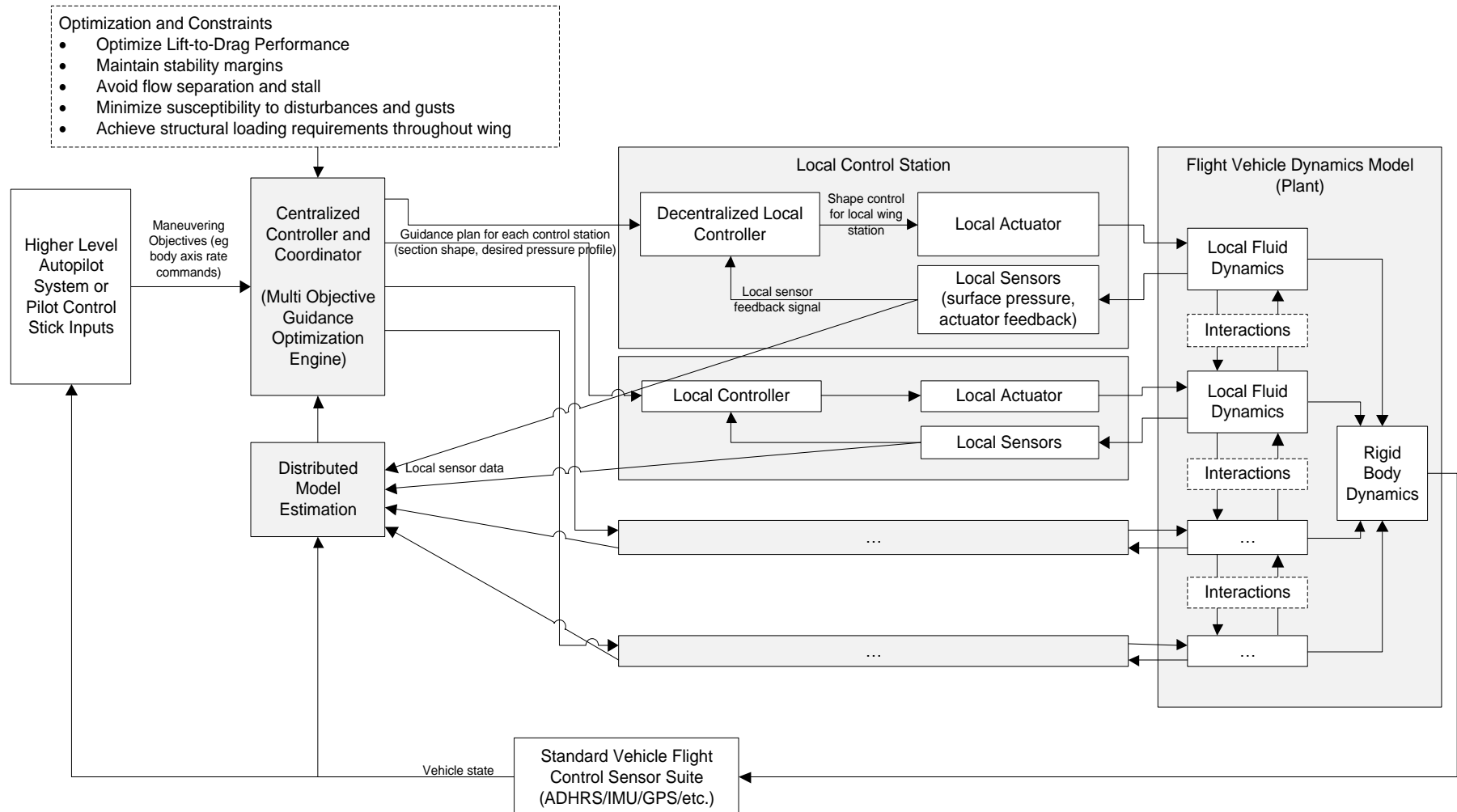
- Physics-Based Model (per vertex/edge)

- Inviscid 2D airfoil analysis using steady-state vortex-panel method to compute  $C_p$  distribution and  $C_L$  per unit section
- Induced drag from finite wing theory using trailing edge vortices
- Viscous skin friction drag needs to be determined (currently researching)
- Separation drag will be ignored, but can be predicted
- Steady solution (non-steady vortex-panel additions will be invested in phase 2)
- Applicable to multiple vehicles and control problems





**NARI**

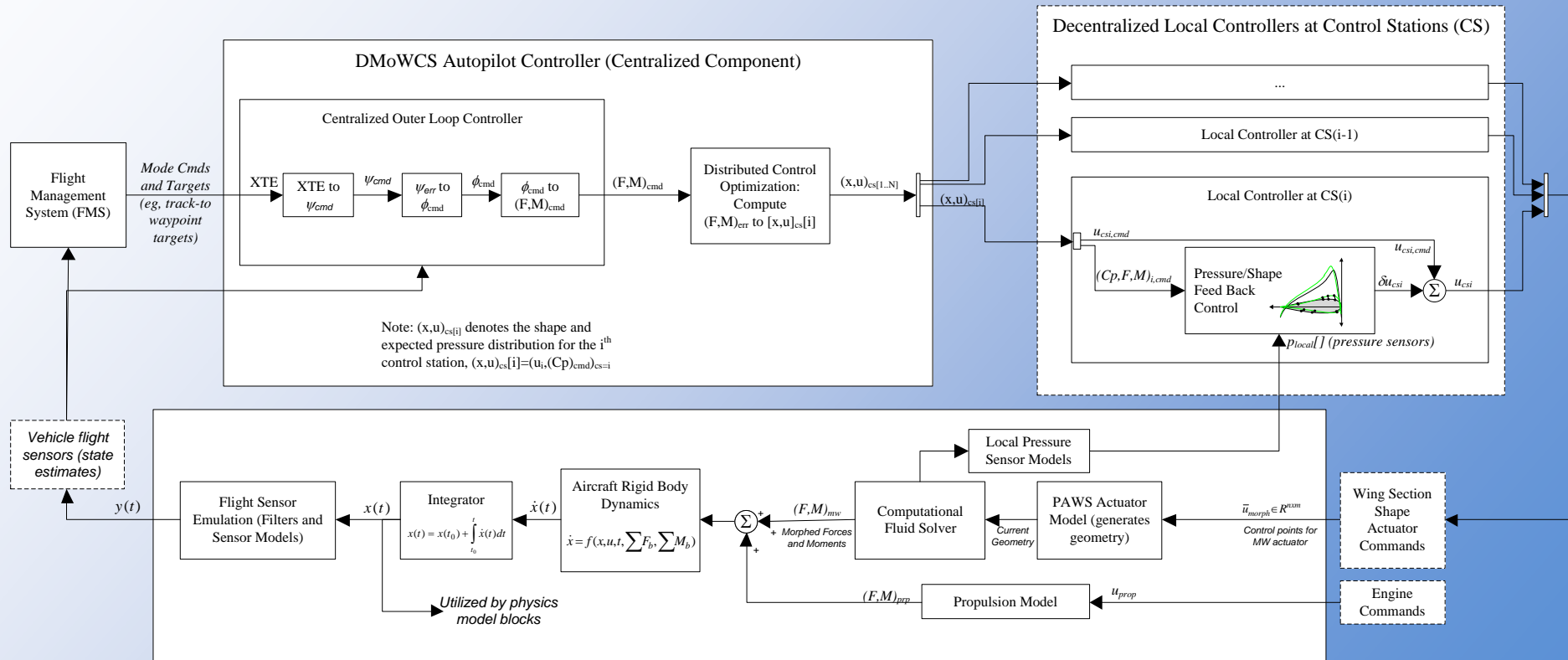


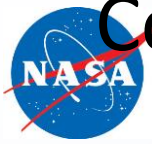


# Parallelized Architecture for Decentralized Flight Modeling and Control

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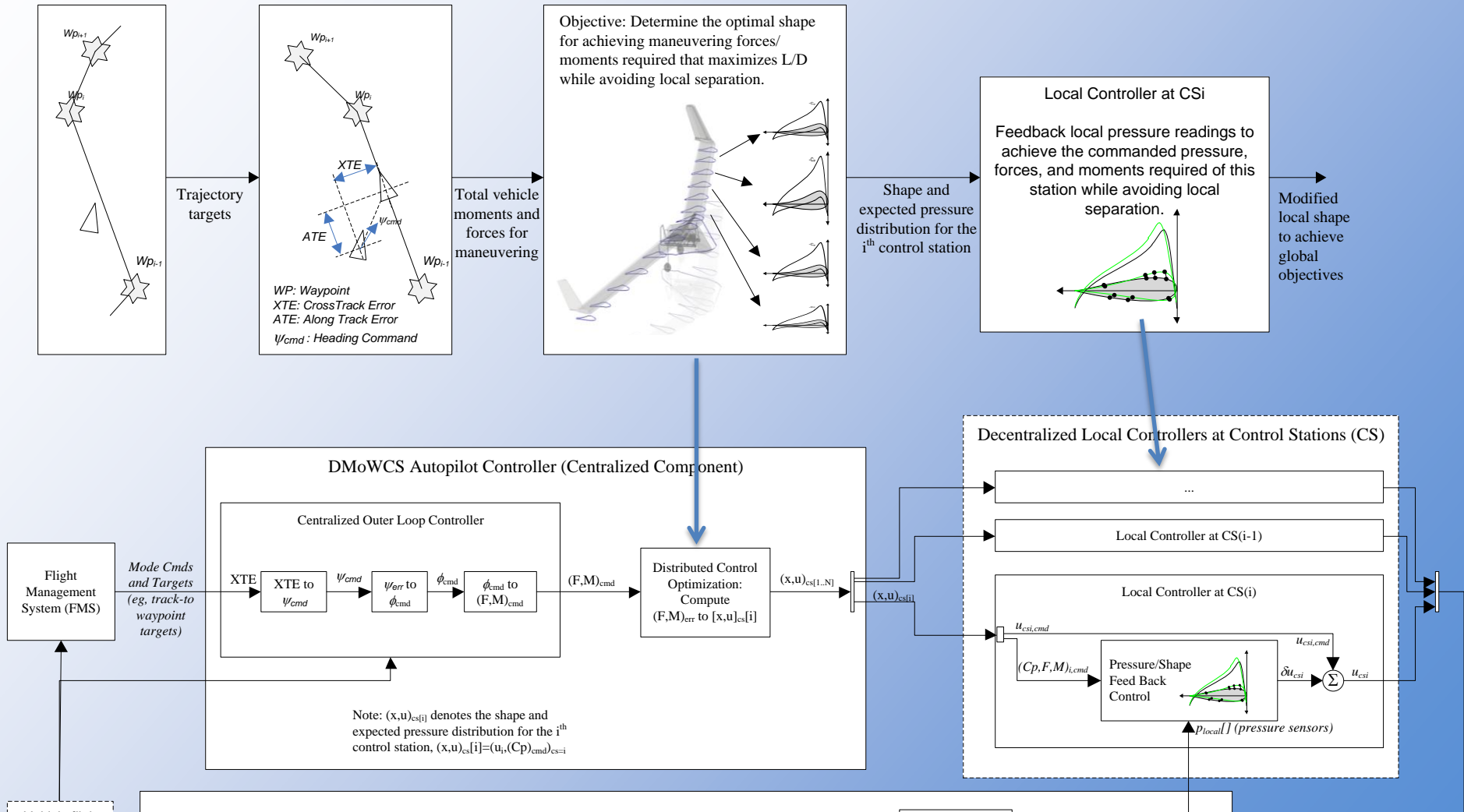
## Simulation Environment





# Control Architecture – Morphing Wing Concept Example

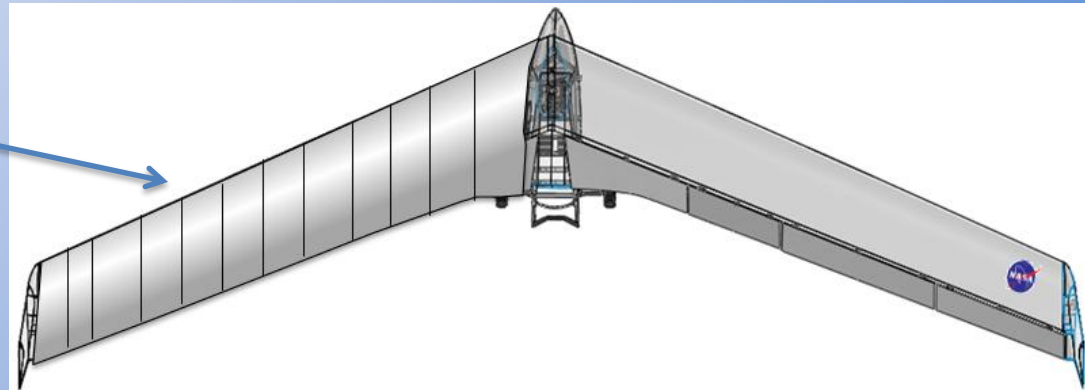
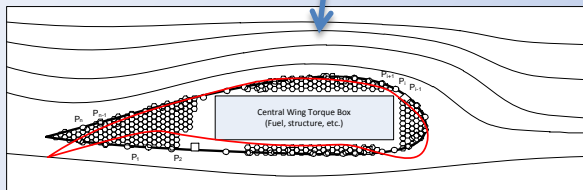
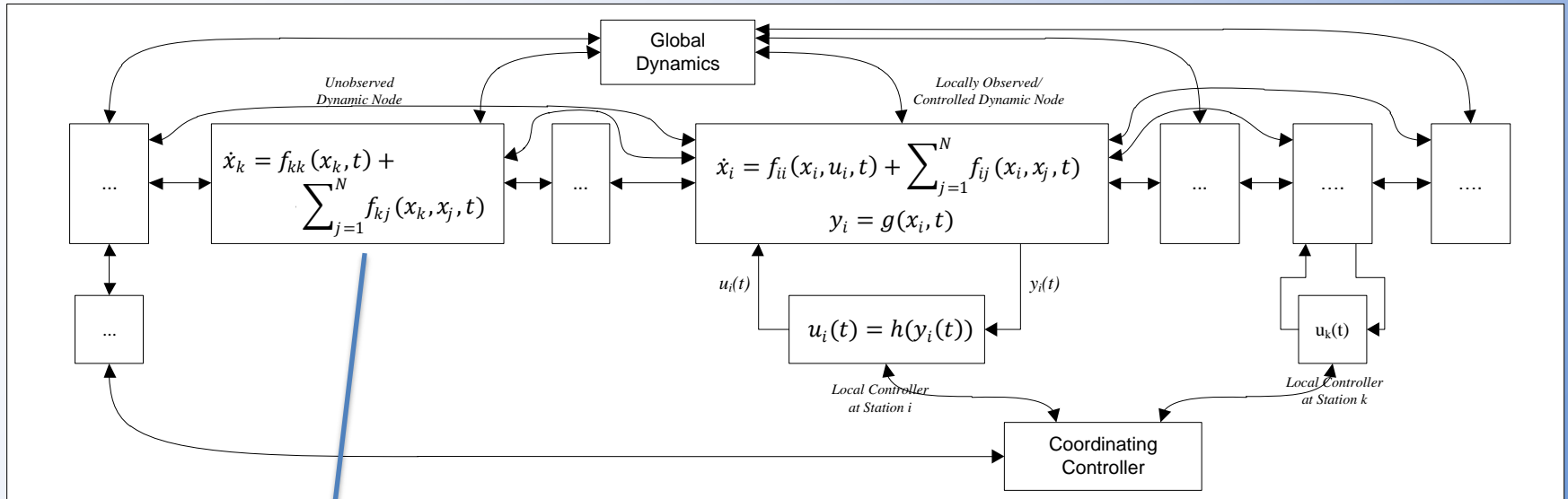
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# Graph-Based Topological Model

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# Physics-Based Element Model

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## Global Integration - 6-DOF Equations of Motion

$$\begin{aligned}\frac{d}{dt}\mathbf{p}_e &= (\tilde{\boldsymbol{\Omega}}_{Eart\ h_e} \mathbf{p}_e) + \mathbf{R}_{b2e} \mathbf{V}_b \\ \frac{d}{dt}\mathbf{v}_b &= -(\boldsymbol{\omega}_b \times \mathbf{v}_b) - (\mathbf{R}_{e2b} \boldsymbol{\Omega}_{Eart\ h_e}^2 + \mathbf{R}_{e2b} \boldsymbol{\Omega}_{Eart\ h_e} \mathbf{R}_{b2e} \boldsymbol{\omega}_b) + \mathbf{R}_{e2b} \mathbf{g}_e + \frac{1}{m} \mathbf{F}_B \\ \frac{d}{dt}\mathbf{q} &= -\frac{1}{2} \tilde{\mathbf{q}} \mathbf{q} \\ \frac{d}{dt}\boldsymbol{\omega}_b &= -\mathbf{J}^{-1} \tilde{\boldsymbol{\omega}}_b \mathbf{J} + \mathbf{J}^{-1} \mathbf{T}_b\end{aligned}$$

$$\mathbf{F}_b = \mathbf{F}_{aero\ b} + \mathbf{F}_{prop\ b} + \mathbf{F}_{morp\ h_b}$$

$$\mathbf{T}_b = \mathbf{T}_{aero\ b} + \mathbf{T}_{prop\ b} + \mathbf{T}_{morp\ h_b}$$

## Assumption

$$\mathbf{F}_b \approx \mathbf{F}_{aero\ b} + \mathbf{M}_{ac2b} (\mathbf{F}_{mw} - \mathbf{F}_{umw})$$

$$\mathbf{T}_b \approx \mathbf{T}_{aero\ b} + \mathbf{M}_{ac2b} (\mathbf{T}_{mw} - \mathbf{T}_{umw})$$

## Alternative

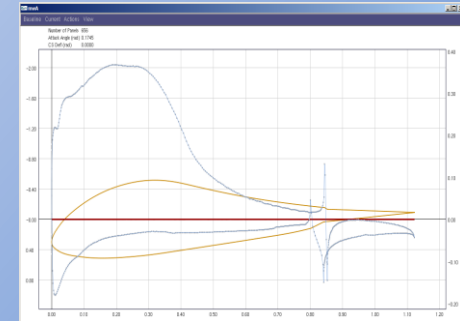
Aerodynamics forces are computed completely by unsteady Vortex-Panel.

## Evaluate $\mathbf{F}_{mw}$ and $\mathbf{T}_{mw}$ through 2D Vortex-Panel Evaluation

$$\mathbf{F}_{ac} = \sum_{i=1}^N \left( P_{\infty} + \left( 1 - \frac{\gamma_i^2}{U_{\infty}^2} \right) \frac{1}{2} \rho_{\infty} U_{\infty}^2 \right) \Delta S_i \hat{n}_i$$

$$\mathbf{T}_{ac} = \sum_{i=1}^N ((P_i - P_{cg}) \times \mathbf{F}_{i\ ac})$$

$\psi(s)$  Stream Function  
 $\gamma_i(s)$  Surface Velocities



Find  $\mathbf{v} = [\tilde{\gamma}, \tilde{\psi}]^T$  by evaluating

$$\begin{bmatrix} K_{11} & K_{12} & \dots & K_{1N} & 1 \\ K_{21} & K_{22} & & K_{2N} & 1 \\ \vdots & & \ddots & \vdots & \vdots \\ K_{N1} & K_{N2} & \dots & K_{NN} & 1 \\ 1 & 0 \dots & \dots & 0 & 1 \end{bmatrix}_{(N+1) \times (N+1)} \begin{bmatrix} \gamma_1 \\ \gamma_2 \\ \vdots \\ \gamma_N \\ \tilde{\psi} \end{bmatrix}_{(N+1)} = \begin{bmatrix} y_1 U_{\infty} \cos \alpha - x_1 U_{\infty} \sin \alpha \\ y_2 U_{\infty} \cos \alpha - x_2 U_{\infty} \sin \alpha \\ \vdots \\ y_N U_{\infty} \cos \alpha - x_N U_{\infty} \sin \alpha \\ 0 \end{bmatrix}_{(N+1)}$$

$$K_{ij} = \frac{1}{2\pi} \left\{ \frac{1}{2} [x_{j+1} \ln(x_{j+1}^2 + y_{j+1}^2) - x_j \ln(x_j^2 - y_j^2)] - (x_{j+1} - x_j) + y_j \left[ \tan^{-1} \left( \frac{y_j}{x_j} \right) - \tan^{-1} \left( \frac{y_{j-1}}{x_{j-1}} \right) \right] \right\} \quad \text{for } i$$

Where

$$K_{ii} = \frac{\Delta S_i}{2} \left( \ln \left( \frac{\Delta S_i}{2} \right) - 1 \right) \quad \text{for } i = j$$





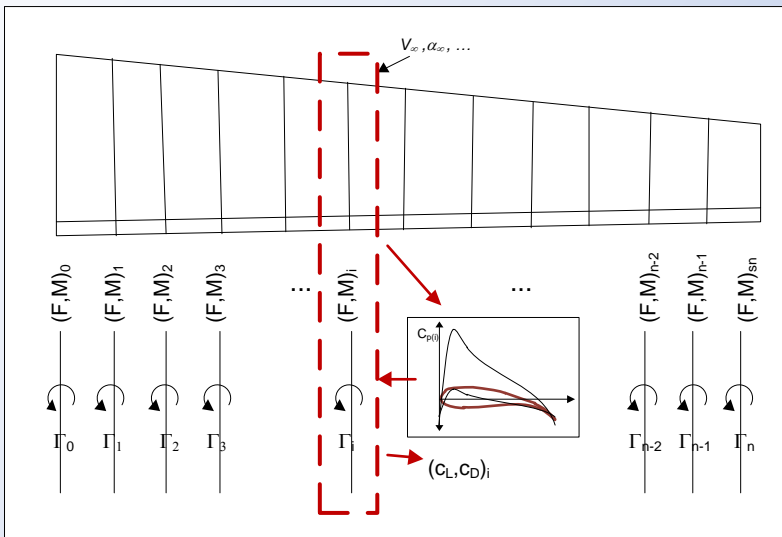
# Physics-Based Model (per-vertex) – Drag

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- Capture major components of drag

$$\text{Drag : } D = D_{\text{induced}} + D_{\text{skin\_fric}} + D_{\text{separation}} + \dots$$

- Approximate 3D induced effects using trailing vortices



- Fundamental equation of finite-wing theory

$$\alpha_a(y_0) = \left( \frac{2\Gamma}{m_0 V_\infty c} \right) y_0 + \frac{1}{4\pi V_\infty} \int_{-b/2}^{b/2} \frac{(d\Gamma/dy)_{\text{wing}}}{y_0 - y} dy$$

- Fourier series for arbitrary circulation distribution

$$\Gamma = \frac{1}{2} m_{0s} c_s V_\infty \sum_{n=1}^{\infty} A_n \sin(n\theta)$$

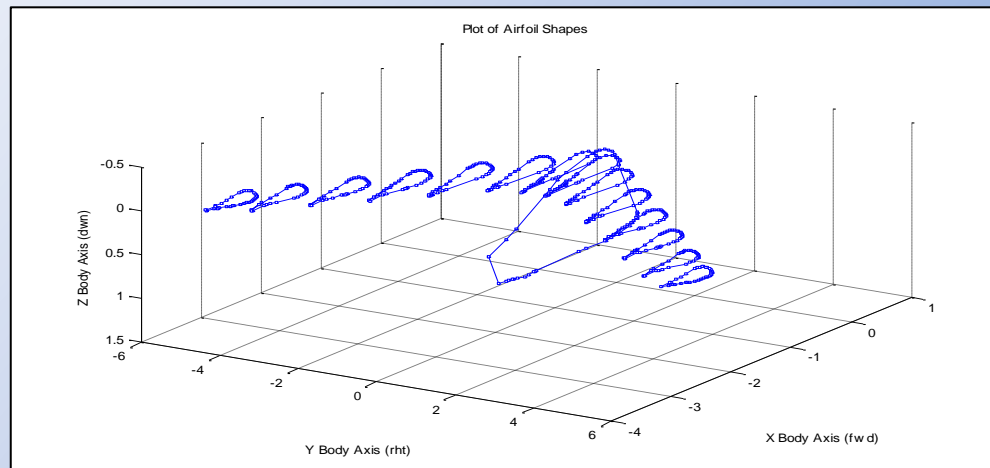
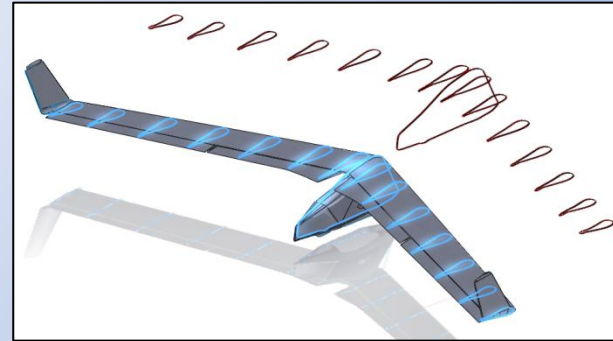
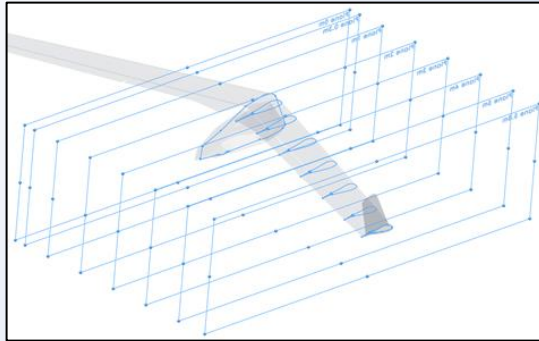
- Numerical approach in (Phillips, 2004)

- Researching incorporate skin friction model



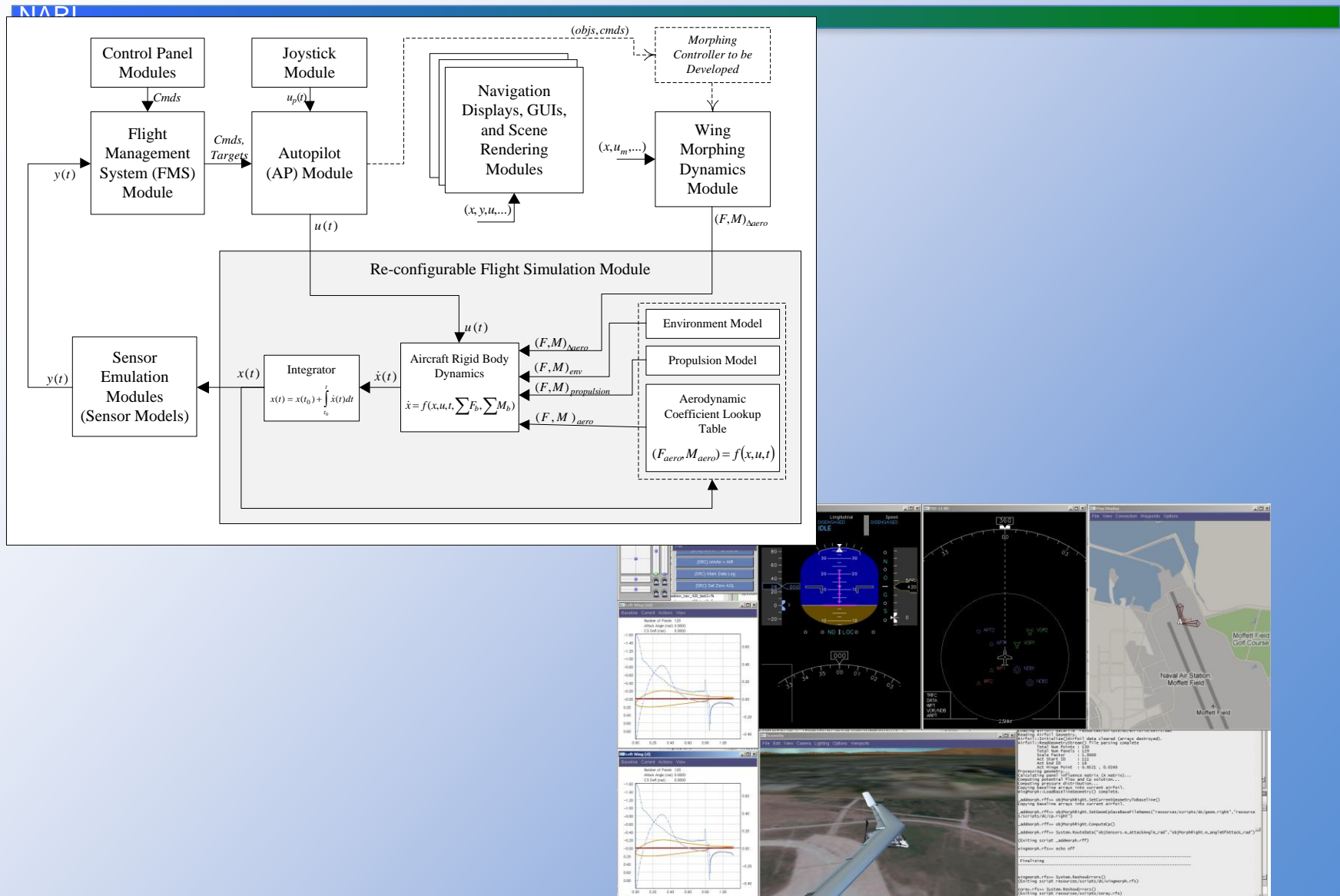
# Modeling of the Swift UAS

NARI





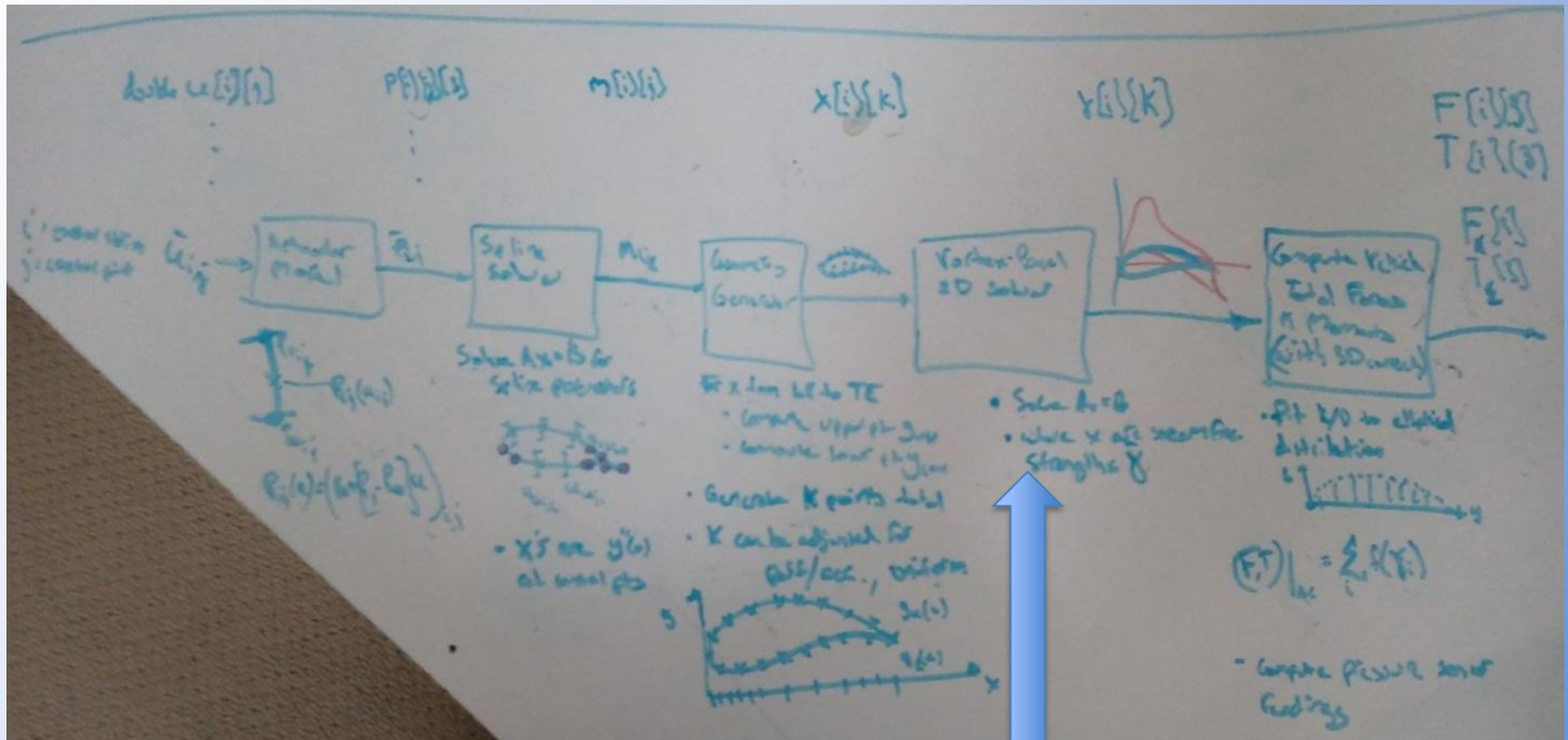
# Simulation in Reflection Architecture





# Real-Time Physics Processing Pipeline

NARI



Optimized on GPU



# Real-Time Optimization Algorithm

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- Propose new Random Subcomplement Search Tree (RST) Framework
  - Approach inspired by random root-tree and probabilistic roadmaps
  - Requires fast evaluation of model dynamics
  - Research goal: continue to formalize approach, parallelized algorithms for faster implementation with more complex models





# RST - Problem Formulation

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Given a system  $\mathcal{S}$  where  $f: \mathcal{X} \times \mathcal{U} \times \mathcal{T} \rightarrow \mathbb{R}^n$ ,  $h: \mathcal{X} \times \mathcal{T} \rightarrow \mathcal{Y}$ , state space  $x \in \mathcal{X} \subseteq \mathbb{R}^n$ , input space  $u \in \mathcal{U} \subseteq \mathbb{R}^m$ , output space  $y \in \mathcal{Y} \subseteq \mathbb{R}^p$ , and time is defined over the convex interval  $t \in \mathcal{T} \subseteq (0..t_f)$ .

$$\mathcal{S}: \begin{cases} \dot{x}(t) = f(x(t), u(t), t) \\ y(t) = h(x(t), t) \end{cases}$$

Given constraints where  $C_{e_i}, C_{i_i}: \mathcal{X} \times \mathbb{R}^n \times \mathcal{U} \times \mathcal{T} \rightarrow \mathbb{R}$

$$\begin{aligned} \mathcal{C} &= \{C_e, C_i\} \\ C_{e_i}(x, \dot{x}, u, t) &= 0 \\ C_{i_i}(x, \dot{x}, u, t) &< 0 \end{aligned}$$

Given performance objectives  $J$ , where  $L = [L_1..L_{n_L}]^T$ , where  $\phi, L_i: \mathcal{X} \times \mathcal{U} \times \mathcal{T} \rightarrow \mathbb{R}$

$$J(x, u, t) = \phi(x(t_f), t_f) + \sum_{i=1}^{n_L} \int_0^{t_f} L_i(x, u, \tau) d\tau$$

Find the optimal trajectory  $(x, u)$  over time  $\tau$  that satisfies

$$u^* = \underset{u}{\operatorname{argmin}}(J(x, u, t))$$

subject to constraints in  $\mathcal{C}$



# RST Approach

NARI

## Dynamical System

$$\mathcal{S}: \begin{cases} \dot{x}(t) = f(x(t), u(t), t) \\ y(t) = x(t) \end{cases}$$

## Constraints

$$C = \{C_e, C_i\}$$

$$C_{e_i}(x, \dot{x}, u, t) = 0$$

$$C_i(x, \dot{x}, u, t) \leq 0$$

## Performance Objectives

$$J(x, u, t) = \phi(x(t_f), t_f) + \sum_{i=1}^{n_L} \int_0^{t_f} L_i(x, u, \tau) d\tau$$

## Problem

$$\text{Find } u^* = \underset{u}{\operatorname{argmin}} (J(x, u, t))$$

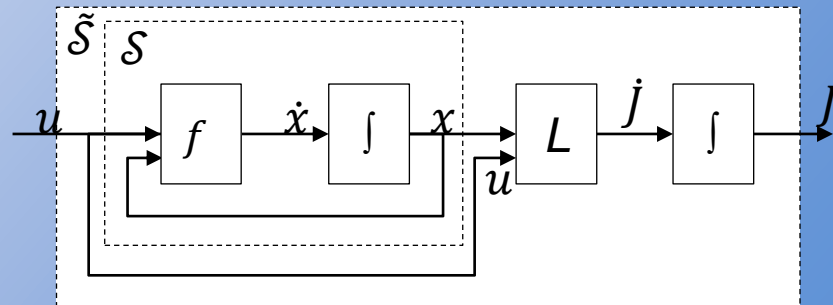
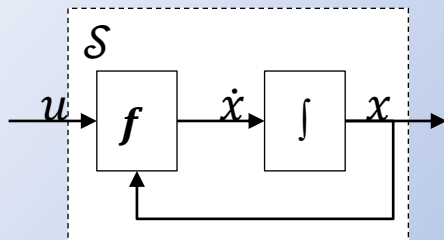
subject to constraints in C

## Augmented System

$$\tilde{\mathcal{S}}: \begin{cases} \dot{\tilde{x}} = \begin{bmatrix} \dot{x} \\ j' \end{bmatrix} = \begin{bmatrix} f(x, u, t) \\ \|L(x, u, t)\|_1 \end{bmatrix} \\ y_{\tilde{\mathcal{S}}} = [J'] = [J'(t)] \end{cases}$$

## Augmented Problem

Find  $u^* = \underset{u}{\operatorname{argmin}} (y_{\tilde{\mathcal{S}}}[0:t_f: x_0: u])$   
subject to constraints in C





# Subcomplement Systems

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## Subcomplement System

Define goal subspace  $\mathcal{X}_G$ , often  $\mathcal{X}_G \subseteq \mathcal{X}$

Let  $x_c \in \mathcal{X}_c$

Let  $u_c \in \mathcal{U}_c = \mathcal{X} \times \mathcal{X}_G$

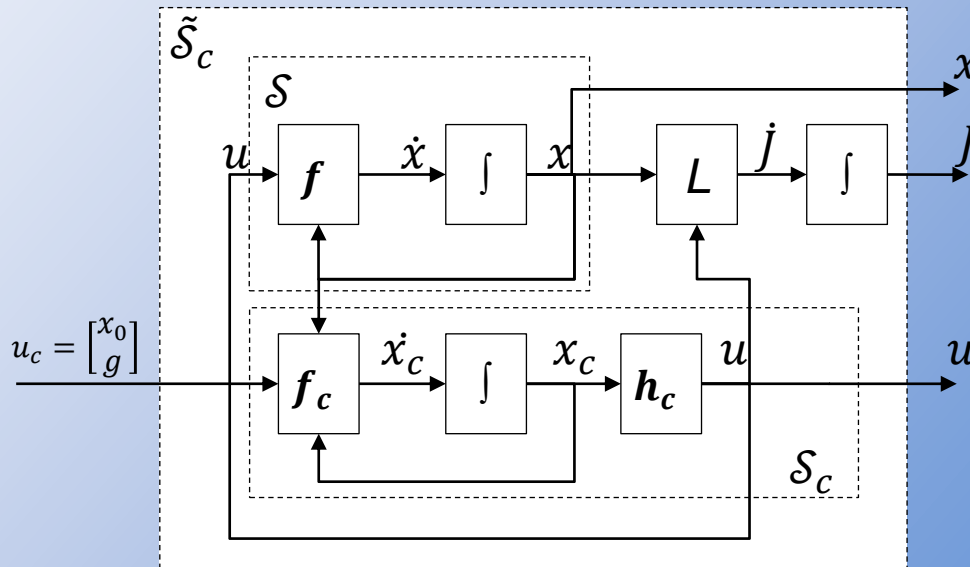
Let  $y_c \in \mathcal{Y}_c = \mathcal{X} \times \mathcal{U} \times \mathbb{R}$

Define the subcomplement system to be

$$\mathcal{S}_c: \begin{cases} \dot{x}_c = [f_c(x_c, u_c, t)] \\ y_c = [u] = [h_c(x_c, u_c, t)] \end{cases}$$

## Augmented Subcomplement System

$$\tilde{\mathcal{S}}_c: \begin{cases} \begin{bmatrix} \dot{x} \\ \dot{x}_c \\ \tilde{j} \end{bmatrix} = \begin{bmatrix} f(x, u, t) \\ f_c(x_c, u_c, t) \\ \|L(x, u, t)\|_1 \end{bmatrix} \\ \begin{bmatrix} u \\ x \\ J \end{bmatrix} = \begin{bmatrix} h_c(x_c, u_c, t) \\ x \\ J \end{bmatrix} \end{cases}$$





# Search Tree Algorithm

NARI

- Let the search tree  $\mathcal{T} = (V, E)$  be defined as a set of vertices  $\mathcal{V} = (\mathcal{X}, \mathcal{U}, \mathcal{T}, \mathbb{R})$  where a vertex  $v_i \in \mathcal{V}$  given by  $v_i = (x(t_i), u(t_i), J(x_i, u_i, t_i), t_i)$ , and edges  $E = \langle V, V \rangle$  be an ordered set of vertices

## Algorithm 1. BuildOptimizationTree ( $x_0, \mathcal{G}, C$ )

Input:  $x_0$ : Start state,  $\mathcal{G}$ : Augmented subcomplement system, C: Constraint set, N: search depth

Variables:  $\mathcal{T}$ : Tree, (v,  $v_l$ ,  $v^*$ ): Vertex (current, leaf, best)

1.  $\mathcal{T} \leftarrow \text{InitTree}(x_0)$
2.  $v^* \leftarrow \emptyset$
3. while ( not StopCondition() ) do
4.    $g \leftarrow \text{RandomGoalPoint}()$
5.    $v \leftarrow \text{RandomTreeVertex}(\mathcal{T}, g, C)$
6.    $v_l \leftarrow \text{GenerateBranch}(\mathcal{G}, v, g, C)$
7.    $v^* \leftarrow \text{StoreBestAtDepth}(v^*, v_l, N)$
8. End while

## Algorithm 2. GenerateBranch ( $\mathcal{T}, \mathcal{G}, v, g, C$ )

Input:  $\mathcal{T}$ : Tree,  $\mathcal{G}$ : Start vertex, v: Start vertex, g: Goal vertex, C: Constraint set

Variables: Tree  $\mathcal{T}$   
Vertex  $v'$   
Branch b

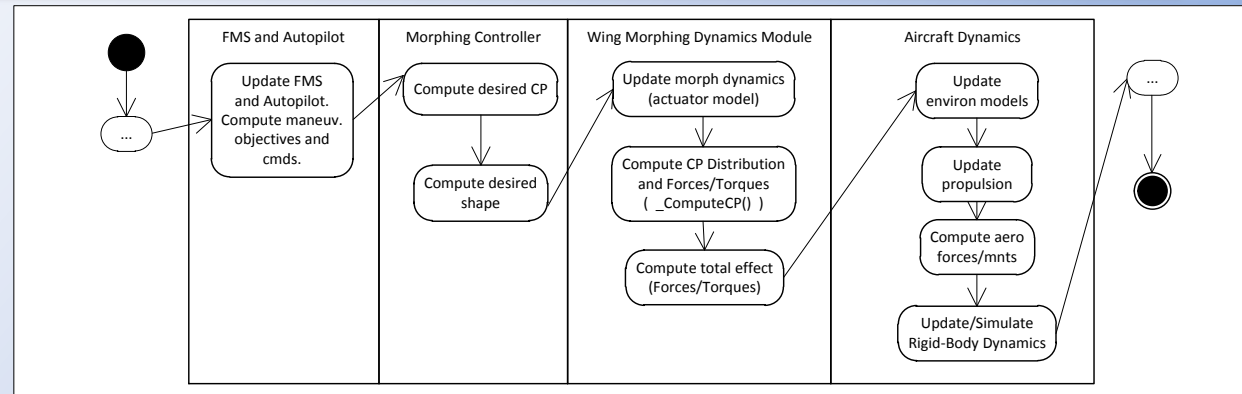
1.  $b \leftarrow \text{FwdIntegrate}(\mathcal{G}, v', g)$
2.  $b \leftarrow \text{Trim}(b, C)$
3. if (  $b \neq \emptyset$  )
4.    $\text{TreeAdd}(\mathcal{T}, v, b)$
5. End if



# Many-Core Optimization

NARI

- Optimization study implemented vortex-panel solver on many-core hardware
- Target: NVIDIA Quadro FX 3700 GPU on Dell Precision M6400



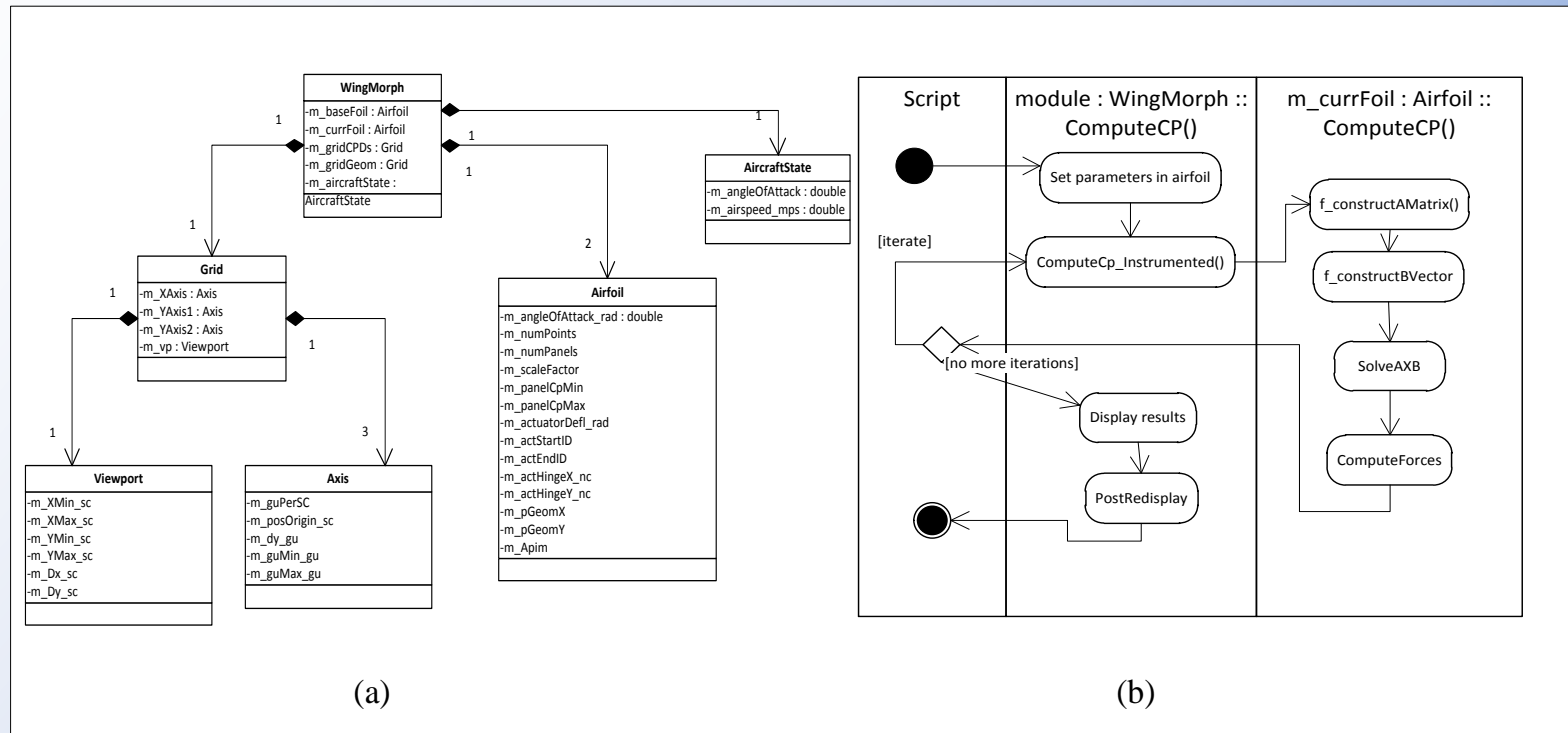
Device 0	Quadro FX 3700M
CUDA Driver Version / Runtime Version	4.0 / 4.0
CUDA Capability Major/Minor version number:	1.1
Total amount of global memory:	966 MBytes (1013383168 bytes)
Number of Multiprocessors	16
CUDA Cores/MP	8
Number of CUDA Cores	128
GPU Clock Speed:	1.38 GHz
Memory Clock rate:	799.00 Mhz
Memory Bus Width:	256-bit
L2 Cache Size:	
Max Texture Dimension Size (x,y,z)	1D=(8192), 2D=(65536,32768), 3D=(2048,2048,2048)
Max Layered Texture Size (dim) x layers	1D=(8192) x 512, 2D=(8192,8192) x 512
Total amount of constant memory:	65536 bytes
Total amount of shared memory per block:	16384 bytes
Total number of registers available per block:	8192
Warp size:	32
Maximum number of threads per block:	512
Maximum sizes of each dimension of a block:	512 x 512 x 64
Maximum sizes of each dimension of a grid:	65535 x 65535 x 1
Maximum memory pitch:	2147483647 bytes





# Many-Core Optimization

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Class Structure (a) and Update Activity in WingMorph::ComputeCP and Airfoil::ComputeCP



# Many-Core Optimization

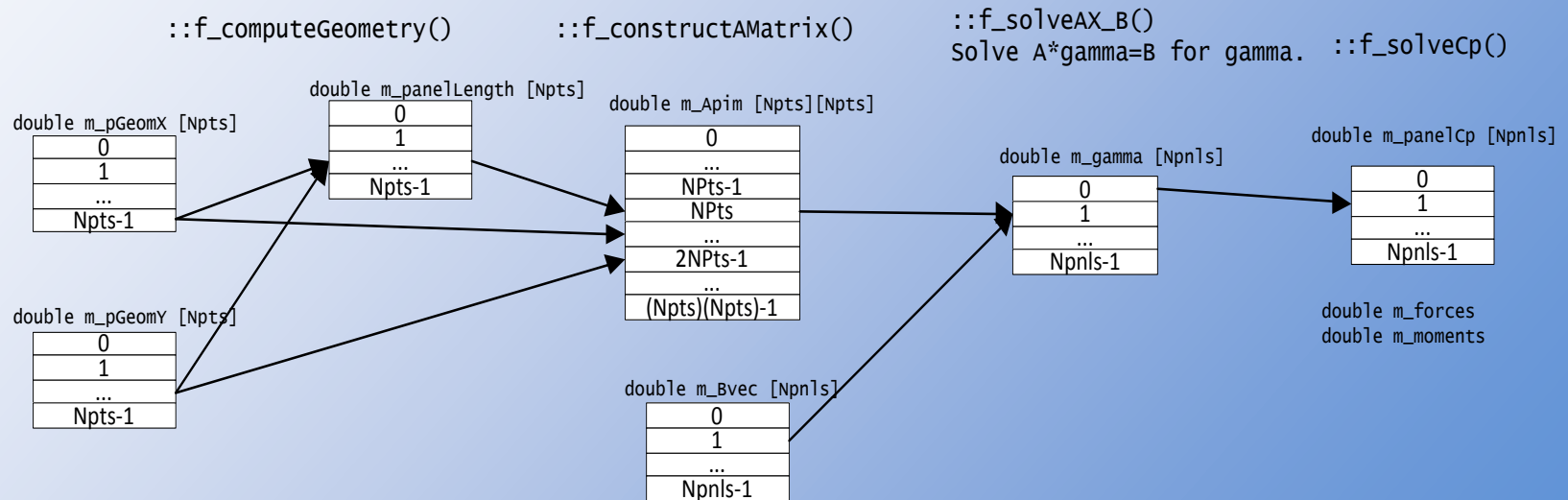
NARI

Table 1. Algorithm and Complexity

Step	Function	Description	Complexity
1	<code>_ComputeGeometry()</code>	Compute geometric arrays <code>panelLength[]</code> , <code>dX[]</code> , <code>dY[]</code>	$O(N)$
2	<code>_ConstructAMatrix()</code>	Construct A matrix and B vector. Baseline uses Gaussian Elimination	$O(N^2)$
3	<code>_SolveAXB()</code>	Solve $Ax=b$ for x	$O(N^3)$
4	<code>_SolveCP()</code>	Solve for pressure distribution, sum total force and moment	$O(N)$

## Memory Structure

`Airfoil::computeCp()`

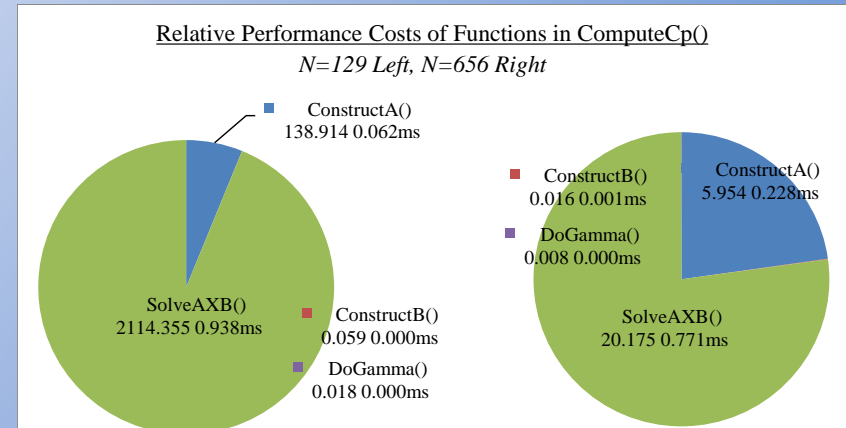
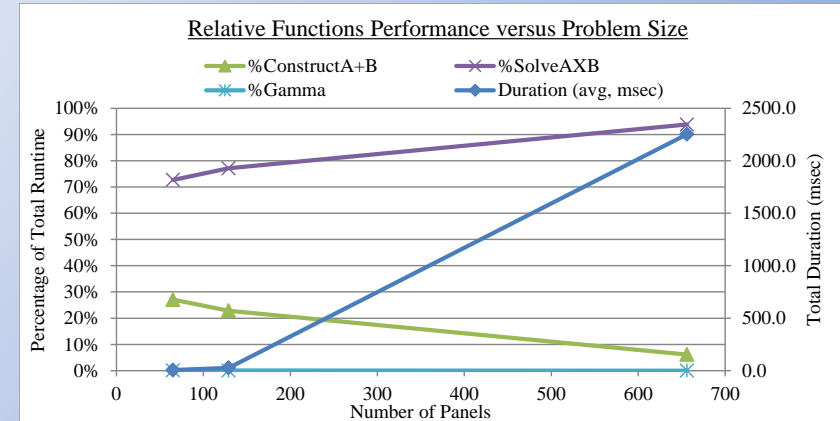




# Many-Core Optimization

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- Analyzed baseline performance as function of number of panels
- The template for each function is the same.
  - Convert double arrays into floats
  - Copy input vectors to device memory
  - Perform kernel array operation
  - Copy resulting device memory to float array in host memory
  - Convert float array back to doubles
- The  $Ax=b$  operation was hand-coded using a Gaussian Elimination algorithm (not optimal for implementation)





# Many-Core Optimization

NARI

- Initial optimization resulted in 35.5 times improvement on simple study
- Optimization focus in grey, cost for evaluating 200 airfoil sections with 656 panels each

Function (time in sec)	Original	Opt A	Opt B	Opt C	Opt D
(top)	6063.7	418.9	375.4	466.8	159.6
ComputeCP	5389.7	437.6	470.1	379.2	185.0
+ConstructA	231.2	27.1	14.7	10.2	10.9
+ConstructB	0.1	0.0	0.0	0.0	0.0
+SolveAXB	5569.6	485.8	455.1	429.6	157.1
+ComputeGamma	38.3	0.0	0.0	0.0	0.0
Total	5657.2	418.9	375.4	466.8	159.6
Improvement (x original)		13.5	15.1	12.1	35.5
Time to 10 sections/50 panels	21.56	1.60	1.43	1.78	0.61



# TECHNICAL DETAILS AND ACCOMPLISHMENTS

## PART III – MORPHING WING STUDY

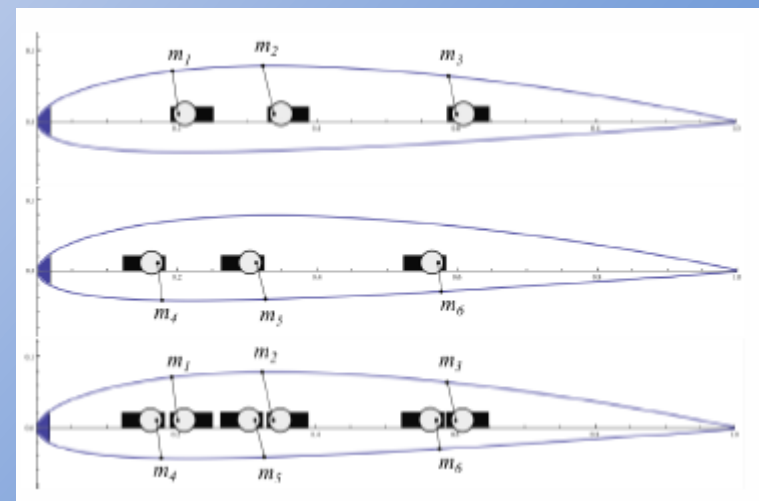
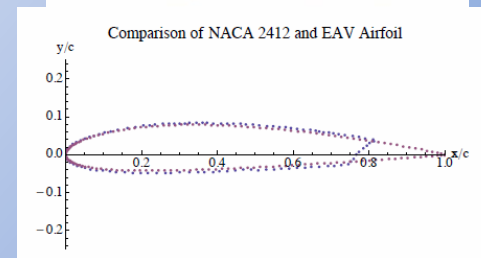




# 2D Morphing Wing Study

NARI

1. Developed morphing wing actuator prototype on a small NASA UAV
  - NASA EAV, a 1/4 scale Cessna 182
  - Intuitively placed servomotors and control points
2. Develop mathematical model of morphing wing actuator geometry, response and characteristics
  - Used NACA 2412 as baseline airfoil
  - Measured actuator speed and characteristics from prototype
  - Modeled using 6 control points
  - Top control points: 5-10% chord length
  - Bottom control points: 0-6% chord length
  - Used natural splines for interpolation between control points



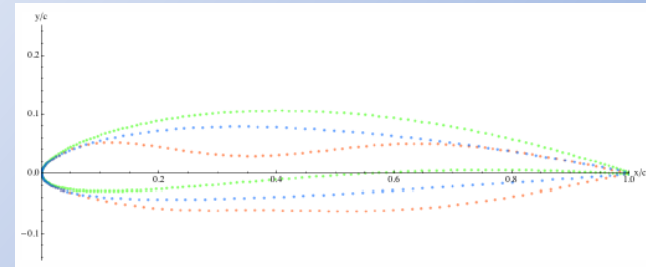


# 2D Morphing Wing Study

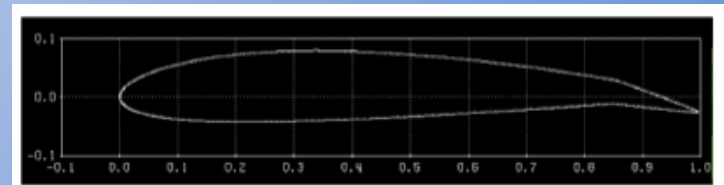
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## 3. Generate database of performance versus actuator position for airfoil

- Steady-state 2D analysis with X-FOIL
- Stored resulting CL, CM, CD for each data point
- Resulting database is highly nonlinear and non-convex over CL, CM, CD
- Generated second database with X-FOIL control surface function



Parameter	Baseline/ Cruise Condition	Min	Max	Delta
Attack angle	5 deg	0 deg	15 deg	1 deg
Speed	20.5 m/s (40 knots)	-	-	-
m1		5%	10%	0.50%
m2		5%	10%	0.50%
m3		5%	10%	0.50%
m4		0%	6%	0.50%
m5		0%	6%	0.50%
m6		0%	6%	0.50%



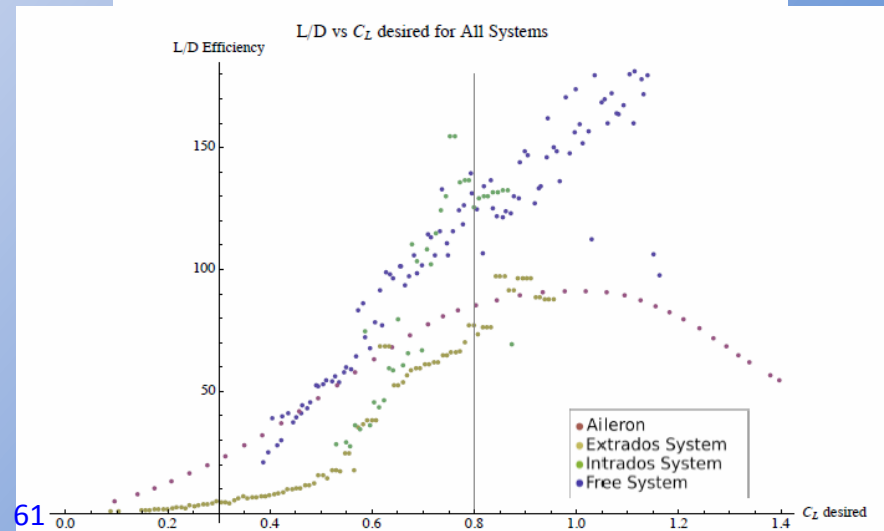
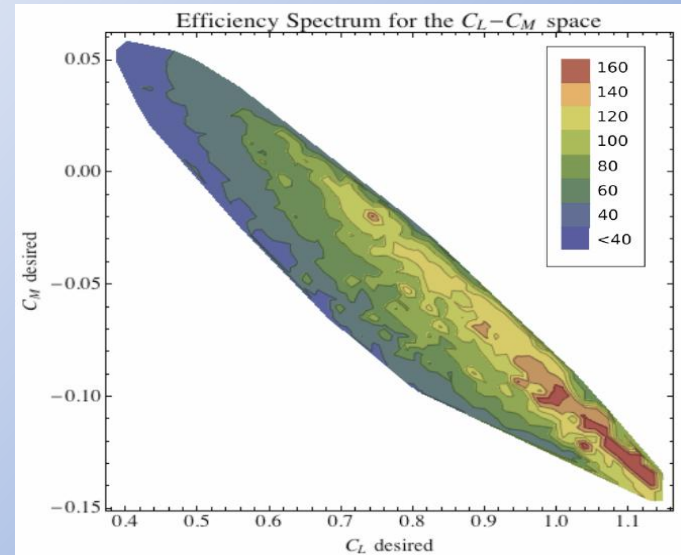


# 2D Morphing Wing Study

NARI

## 4. Analyze and optimize database

- Find optimally L/D efficient mapping from desired ( $C_L, C_M$ ) to an actuator vector solution  $u=(m_1, \dots, m_6)$
- Discretize CL-CM space into 100x100 buckets from  $C_L=(0.4, 1.15)$ ,  $C_M=(-0.15, 0.06)$
- Find most efficient actuator combination in each CL-CM bucket

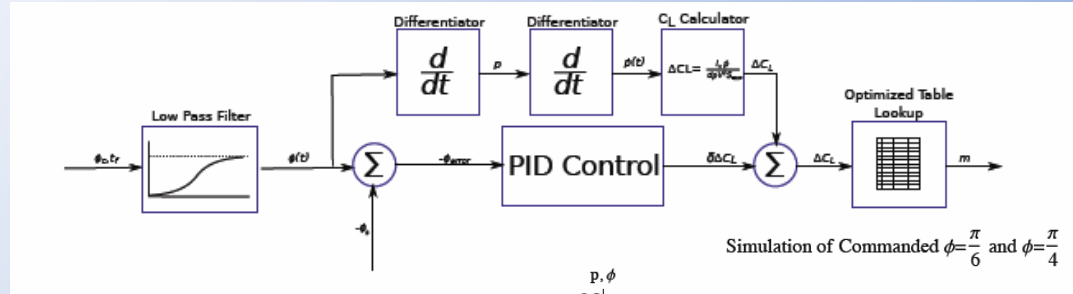




# 2D Morphing Wing Study

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## 5. Design 2D controller to achieve roll angle using differential wing morphing



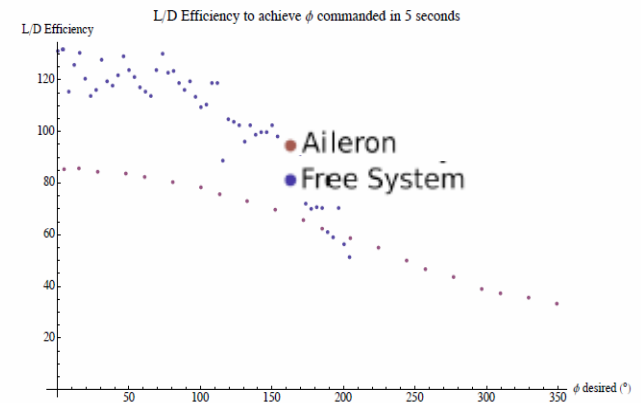
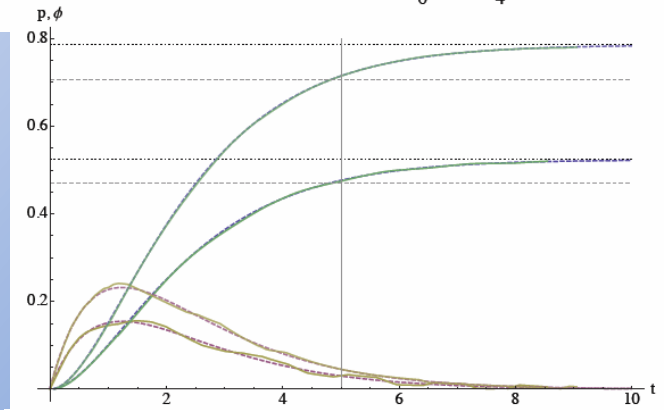
## 6. Test in simulation

$$\dot{\bar{x}} = A\bar{x} + B\bar{u} + C, \quad \bar{x} = [v, p, r, \phi, u, w, q, \theta]$$

$$\begin{pmatrix} \dot{X} \\ \dot{Y} \\ \dot{Z} \end{pmatrix} = \begin{pmatrix} q_\infty S \cos(\beta) (-\cos(\alpha)(C_{D_L} + C_{D_R}) + \sin(\alpha)(C_{L_R} + C_{L_L})) \\ q_\infty S \sin(\beta) (-\cos(\alpha)(C_{D_L} + C_{D_R}) + \sin(\alpha)(C_{L_R} + C_{L_L})) \\ -q_\infty S (\sin(\alpha)(C_{D_L} + C_{D_R}) + \cos(\alpha)(C_{L_L} + C_{L_R})) \end{pmatrix}$$

$$\begin{pmatrix} \dot{L} \\ \dot{M} \\ \dot{N} \end{pmatrix} = \begin{pmatrix} 0 \\ d \\ 0 \end{pmatrix} \times \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}_R + \begin{pmatrix} 0 \\ -d \\ 0 \end{pmatrix} \times \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}_L + \begin{pmatrix} 0 \\ \frac{1}{2} q_\infty S c (C_{M_L} + C_{M_R}) \\ 0 \end{pmatrix}$$

$$C = \begin{pmatrix} q_\infty S \sin(\beta) (-\cos(\alpha)(C_{D_L} + C_{D_R}) + \sin(\alpha)(C_{L_L} + C_{L_R})) \\ dq_\infty S (\sin(\alpha)(C_{D_L} - C_{D_R}) + \cos(\alpha)(C_{L_L} - C_{L_R})) \\ dq_\infty S \cos(\beta) (\cos(\alpha)(-C_{D_L} + C_{D_R}) + \sin(\alpha)(C_{L_L} - C_{L_R})) \\ 0 \\ q_\infty S \cos(\beta) (-\cos(\alpha)(C_{D_L} + C_{D_R}) + \sin(\alpha)(C_{L_L} + C_{L_R})) \\ -q_\infty S (\sin(\alpha)(C_{D_L} + C_{D_R}) + \cos(\alpha)(C_{L_L} + C_{L_R})) \\ \frac{1}{2} c q_\infty S (C_{M_L} + C_{M_R}) \\ 0 \end{pmatrix}$$

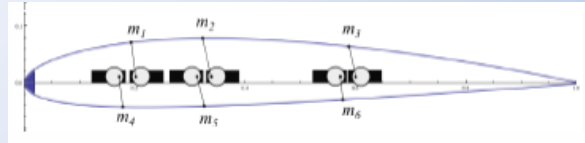




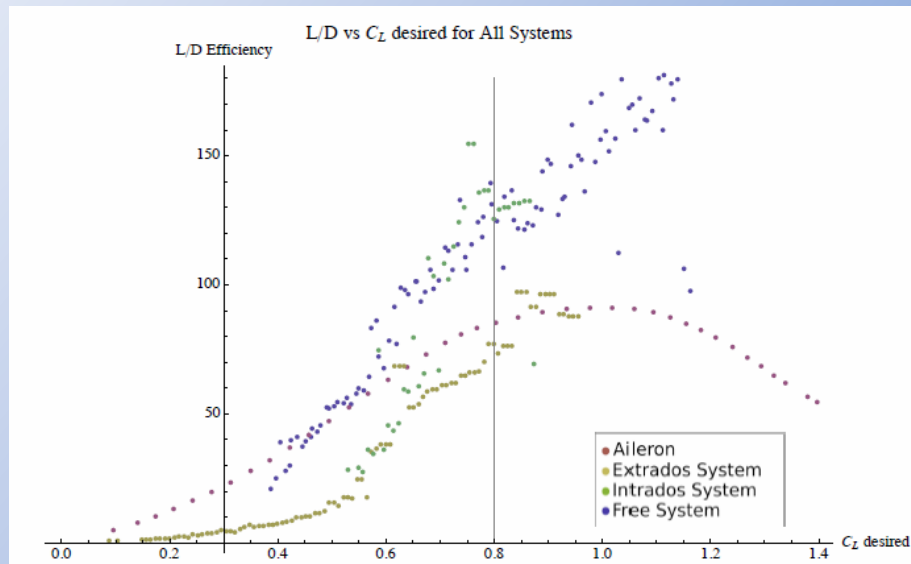
# 2D Morphing Wing Study

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- Coarse 2D study investigated feasibility and expected benefits from concept
  - Real-time distributed individually-actuated control concept
  - Benefits expected to multiply with larger more complex systems



- Results show feasibility and expected L/D improvement
  - L/D improvement around  $\sim 41\%$  across entire (flyable) range, 47% roll maneuvering efficiency improvement

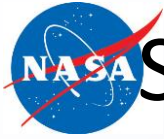






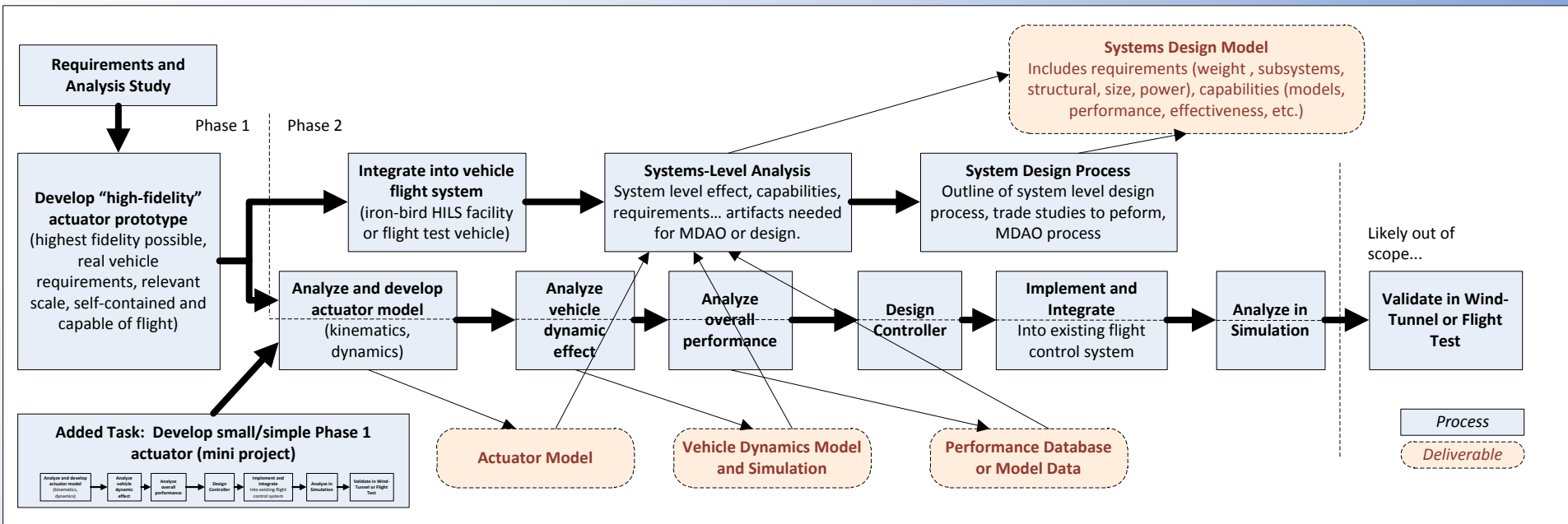
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# PHASE 2 APPROACH AND PLAN



# Summary of Approach and Phase 2 Plan

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[illegible]



# Phase 2 Proposed Plan Details

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- PAWS Prototype Delivery, Analysis and Modeling
  - Complete PAWS prototype, deliver to NASA
  - Develop structural kinematics model of the PAWS prototype actuator
  - Perform vehicle systems-level analysis and requirements
  - Detail incorporation into MDAO process
  - Submit prototype for external review from stakeholders - NASA and Boeing
- DMoWCs Control System Integration
  - Validate and Extend Model
    - Conduct model validation and submit model for external review.
    - Investigate extending model to incorporate dynamic unsteady aerodynamics.
    - Deliverable: modeling library source-code and API
- Integration DMoWCs and actuation model
  - Integrate PAWS actuator model into DMoWCs simulation and control system.
  - DMoWCs components will be adapted for control of the PAWS actuation model.
- Develop distributed sensing and state estimation
  - Distributed estimation was demonstrated on a similar fluid/thermal model for building control. A similar approach will be used in this investigation.



# Phase 2 Proposed Plan Details

NARI

- Conduct optimization and simulation performance studies
  - DMoWCs and PAWS Integration and HILS Testing (I&T)
    - Integrate PAWS prototype into the NASA Swift UAS iron-bird HILS facility.
    - Install PAWS prototype and support hardware into the HILS facility.
    - Integrate DMoWCs into HILS facility, showing closed-loop control of PAWS.
    - Conduct integrated DMoWCs/PAWS hardware-in-the-loop simulation studies.
- Flight Testing DMoWCs and PAWS: Optional Development Path
  - Perform integration of DMoWCs and PAWS
  - Conduct ground test and environment testing
  - Obtain flight permission from flight worthiness board
  - Conduct final flight tests
- Dissemination of Results
  - Fast dissemination of results through the following conference publications: 2012 AIAA Infotech conference (currently pending final review), 2013 AIAA Aerospace Sciences Meeting, 2013 IEEE Aerospace conference
  - Targeting submission to IEEE Trans. on Aerospace and Electronic Systems
  - Final NASA technical report





# Phase 2 Information Dissemination Plan

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- Fast dissemination of results through conference publications
  - 2012 AIAA Infotech conference (currently pending final review)
  - 2013 AIAA Aerospace Sciences Meeting
  - 2013 IEEE Aerospace conference
- Targeting submission to IEEE Trans. on Aerospace and Electronic Systems
- Final NASA technical report
- Project interaction with stakeholders
  - NASA Fixed-Wing (ESAC subtask), Boeing R&T unit, Cessna, MLB



# Summary

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- Phase 1 results showed concepts are feasible
- PAWS prototype on schedule to be completed at end of Phase 1
- NASA small-scale UAV prototype study shows feasibility and performance benefits
- Formalized decentralized control system framework and flight control system architecture
- Showed initial parallelization on many-core architecture
- Implemented model in simulation environment for testing in Phase 2
- Identified Phase 2 stakeholders and infusion plan into NASA ARMD research programs, identified technology commercialization partners (Boeing, Cessna, MLB)



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# Integration and Control of Morphing Wing Structures for Fuel Efficiency/Performance

NARI's ARMD 2011 Phase 1 Seedling Fund Technical Seminar  
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